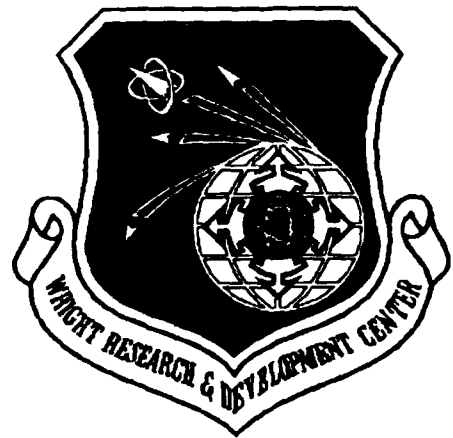


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WRDC-TR-89-2112

**AUTOMATED CODE DEMONSTRATION FOR
COMPRESSOR BLADE STRESSES AND
NATURAL FREQUENCIES**



Laila Abdel-Dayem
Mark Redding

Stress Technology, Inc.
1800 Brighton-Henrietta Town Line Road
Rochester NY 14623

May 1989

Final Report for Period November 1988 to April 1989

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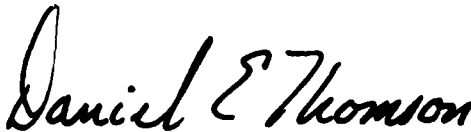


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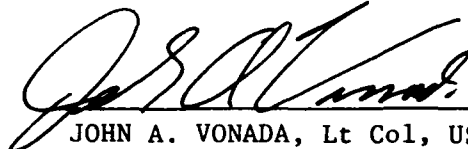
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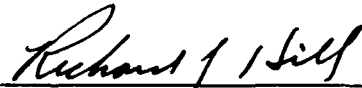


DANIEL E. THOMSON
Project Engineer
Components Branch
Turbine Engine Division



JOHN A. VONADA, Lt Col, USAF
Chief
Components Branch
Turbine Engine Division

FOR THE COMMANDER



RICHARD J. HILL
Acting Deputy for Technology
Turbine Engine Division
Aero Propulsion & Power Directorate

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TABLE OF CONTENTS

1. INTRODUCTION	1
2. FINITE ELEMENT MODEL	2
2.1 User Input	2
2.2 Example	9
3. BLADE ANALYSIS	25
3.1 Steady Stress Analysis	25
3.2 Natural Frequency Analysis	30
3.3 Comparison with Test Results	38
4. CONCLUSION	49
APPENDIX	51

LIST OF FIGURES

	Page
Figure 2.1.1 Typical Airfoil Section Input	4
Figure 2.1.1 Root Side View	6
Figure 2.1.3 Root Front View	7
Figure 2.1.4 Disk Side View	8
Figure 2.2.1 Root Section Front View	11
Figure 2.2.2 Root Section Side View	12
Figure 2.2.3 Disk Data	13
Figure 2.2.4 Example Finite Element Model	17
Figure 2.2.5 Finite Element Model for the Example	18
Figure 2.2.6 Finite Element Model of Root and Disk Section	19
Figure 2.2.7 Finite Element Model for Root	20
Figure 2.2.8 Finite Element Model for Airfoil and Platform	21
Figure 2.2.9 Finite Element Model for Disk Side View	22
Figure 2.2.10 Finite Element Model for Disk Front View	23
Figure 3.1.1 Maximum Nodal Steady Stresses	26
Figure 3.1.2 Maximum Nodal Stresses in Disk	27
Figure 3.1.3 A Different View of Disk Nodal Stresses	28
Figure 3.2.1 Mode Shape 1	32
Figure 3.2.2 Mode Shape 2	33
Figure 3.2.3 Mode Shape 3	34
Figure 3.2.4 Mode Shape 4	35
Figure 3.2.5 Mode Shape 5	36
Figure 3.2.6 Campbell Diagram	37
Figure 3.3.1 Comparison of Test Holograms and Analytical Results for Mode 1	41
Figure 3.3.2 Comparison of Test Holograms and Analytical Results for Mode 2	42
Figure 3.3.3 Comparison of Test Holograms and Analytical Results for Mode 3 ..	43
Figure 3.3.4 Comparison of Test Holograms and Analytical Results for Mode 5	44
Figure 3.3.5 Comparison of Test Holograms and Analytical Results for Mode 6	45

LIST OF FIGURES (CONCLUDED)

Page

Figure 3.3.6	Comparison of Test Holograms and Analytical Results for Mode 8	46
• Figure 3.3.7	Comparison of Test Holograms and Analytical Results for Mode 10	47
• Figure 3.3.8	Comparison of Test Holograms and Analytical Results for Mode 11	48

LIST OF TABLES

	Page
Table 2.2.1 Example Input File	14
Table 2.2.2 Details of Compressor Blade Model	24
Table 3.1.1 Maximum Equivalent Stresses	29
Table 3.2.1 Natural Frequencies for a Single Blade	31
Table 3.3.1 Comparison of Calculated Frequencies and Test Data ...	39
Table 3.3.2 Dynamic Modulus of Prototype TI-6AL-4V Blades	40

1. INTRODUCTION

Accurate predictions of the stresses, natural frequencies and mode shapes of rotating blades for compressors are essential to the performance of aircraft engines. The first objective of this project is to demonstrate that a preprocessor for the modeling of compressor blades with a wedge type root attachment is feasible. A user-friendly program was devised to be used with the minimum possible input that describes the geometry of different components.

The second objective was to use this program in conjunction with BLADE to perform steady stress and natural frequency analyses for a selected example. The BLADE program, which is developed by STI, is a special purpose computer code for steam turbine blade stress and fatigue analysis. This program is sponsored by the Electric Power Research Institute (EPRI). A brief description of BLADE is included in the Appendix.

The results of these analyses were evaluated by their comparison to the ANSYS finite element program results. These results were validated using experimental data provided by the Wright Research and Development Center at WPAFB.

2. FINITE ELEMENT MODEL

A finite element model for the blade and disk attachment is constructed with minimum input information on the part of the user. In this section, the user input is described. An example which describes how the finite element model was generated is given.

2.1 User Input

The user should provide the program with some information about the following:

- ° the vane sections geometry
- ° the root features
- ° the disk geometry
- ° the blade materials
- ° forcing

The input file is a free format ASCII file. It consists of several records. Each record starts with a keyword which describes the input section for which the next set of data belongs to. The first record of the input file is an exception: it contains the title of the analysis, without being preceded by a keyword. In the following, the input file records are described:

Record 1 : **TITLE**

Record 2 : **COVER** - Keyword
IC - Material reference number
R1 - Radius of blade tip trailing edge
R2 - Radius of blade tip leading edge

Record 3 : **AIRFOIL** - Keyword (Figure 2.1.1)
IA - Material reference number
R - Radius of airfoil section
YLE, ZLE - Coordinates of leading edge
YTE, ZTE - Coordinates of trailing edge

NAP - Number of defined airfoil points on the pressure side

$\left. \begin{array}{c} Y(1), Z(1) \\ \vdots \\ Y(2), Z(2) \end{array} \right\}$ Pressure side coordinates

Y(NAP), Z(NAP)

NAS - Number of defined airfoil points on the suction side

$\left. \begin{array}{c} Y(1), Z(1) \\ \vdots \\ Y(2), Z(2) \\ Y(NAS), Z(NAS) \end{array} \right\}$ Suction side coordinates

Note: NAP and NAS do not have to be equal.

Record 3 may be repeated for different airfoil sections up to a maximum of 10 sections.

Record 4 : PLATFORM - Keyword (Figure 2.1.2)

IP - Material reference number

R0 - Radius to the underside of platform

HD - Height of platform at the downstream end

HU - Height of platform at the upstream end

AL - Axial length of platform

CLE - Distance from root centerline to leading edge of platform

CTE - Distance from root centerline to trailing edge of platform

DC - Distance from platform leading edge to the coordinate axis in the axial direction

OPRET - Offset of root centerline from the blade's global coordinate system

RF - Fillet radius of curvature between the airfoil and platform

ANG - Slant angle

ZERO - The number zero (this variable would be needed for curved roots)

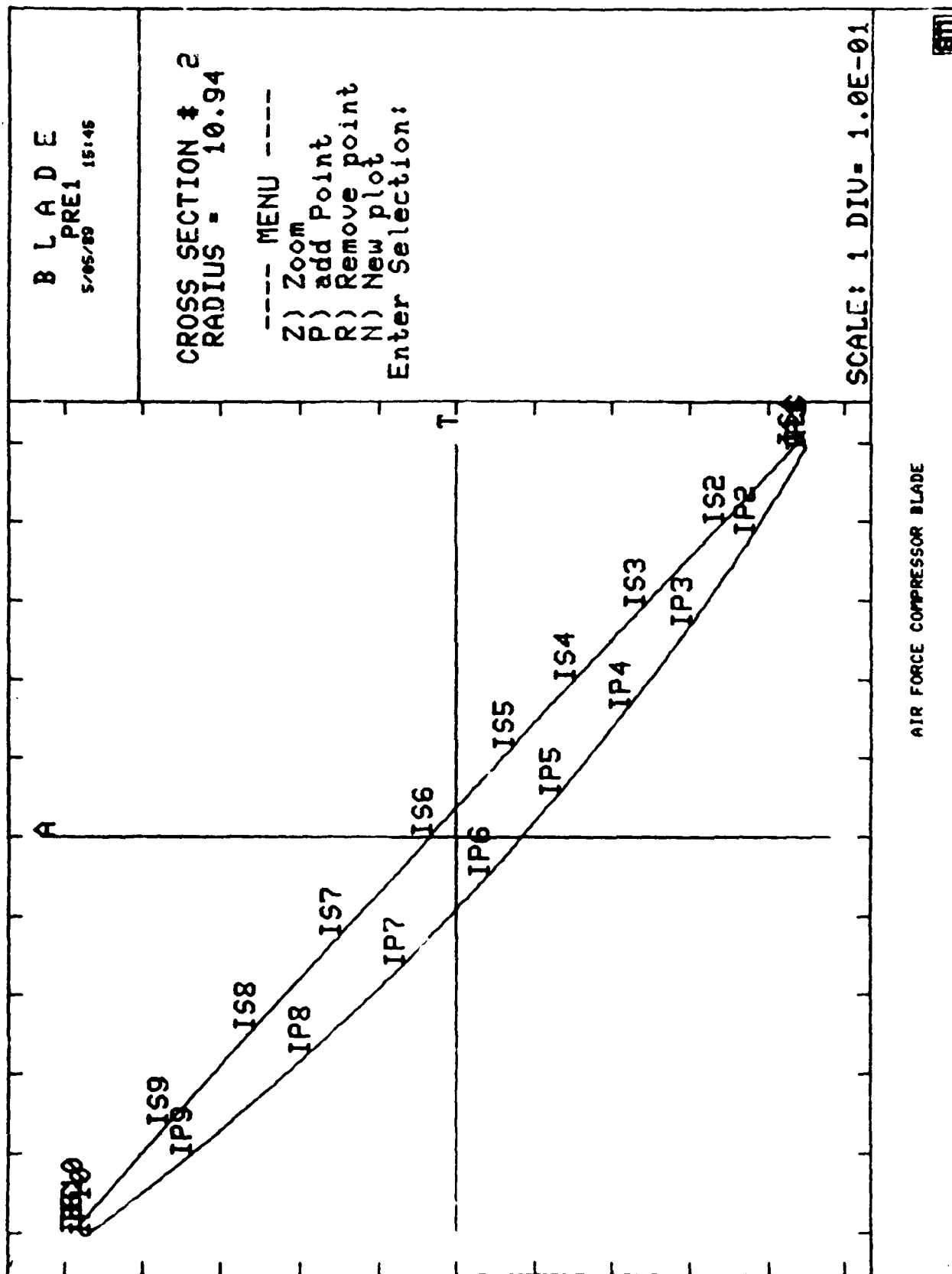


Figure 2.1.1.1: Typical Airfoil Section Input

Record 5 : **ROOT** - Keyword (Figure 2.1.2 and 2.1.3)

ITYPE - Root type number (set to 61)

IR - Material reference number

X1, Y1, ...
 \vdots
 \vdots
X8, Y8 } - Coordinates of input points

R1, R2, - Input radii
R3, R4

VS - Stop width

NP - Number of points defining root end sections

X(1), Z(1)
 \vdots
 \vdots
X(NP), Z(NP) } - Coordinates of end section

Record 6 : **DISC** - Keyword (Figure 2.1.4)

ID - Material reference number

NPD - Number of pair of points describing the disk

X1 (1), Z1 (1), X2 (1), Z2 (1)
 \vdots
 \vdots
X1(NPD), Z1(NPD), X2(NPD), Z2(NPD) } - Coordinates of disk points

Record 7 : **MATERIAL** - Keyword

I1 - Material user reference number

IM - Reference number from material library

TM - Temperature at which material is defined

Record 7 may be repeated for different material types up to a maximum of 10 material types.

Record 8 : **STAGE PARAMETERS** - Keyword

NBLADES - Total number of blades in the stage

NBG - Number of blades per group

NBP - Number of groups to be analyzed

NZ - Number of upstream nozzles

DMFR - Damping ratio

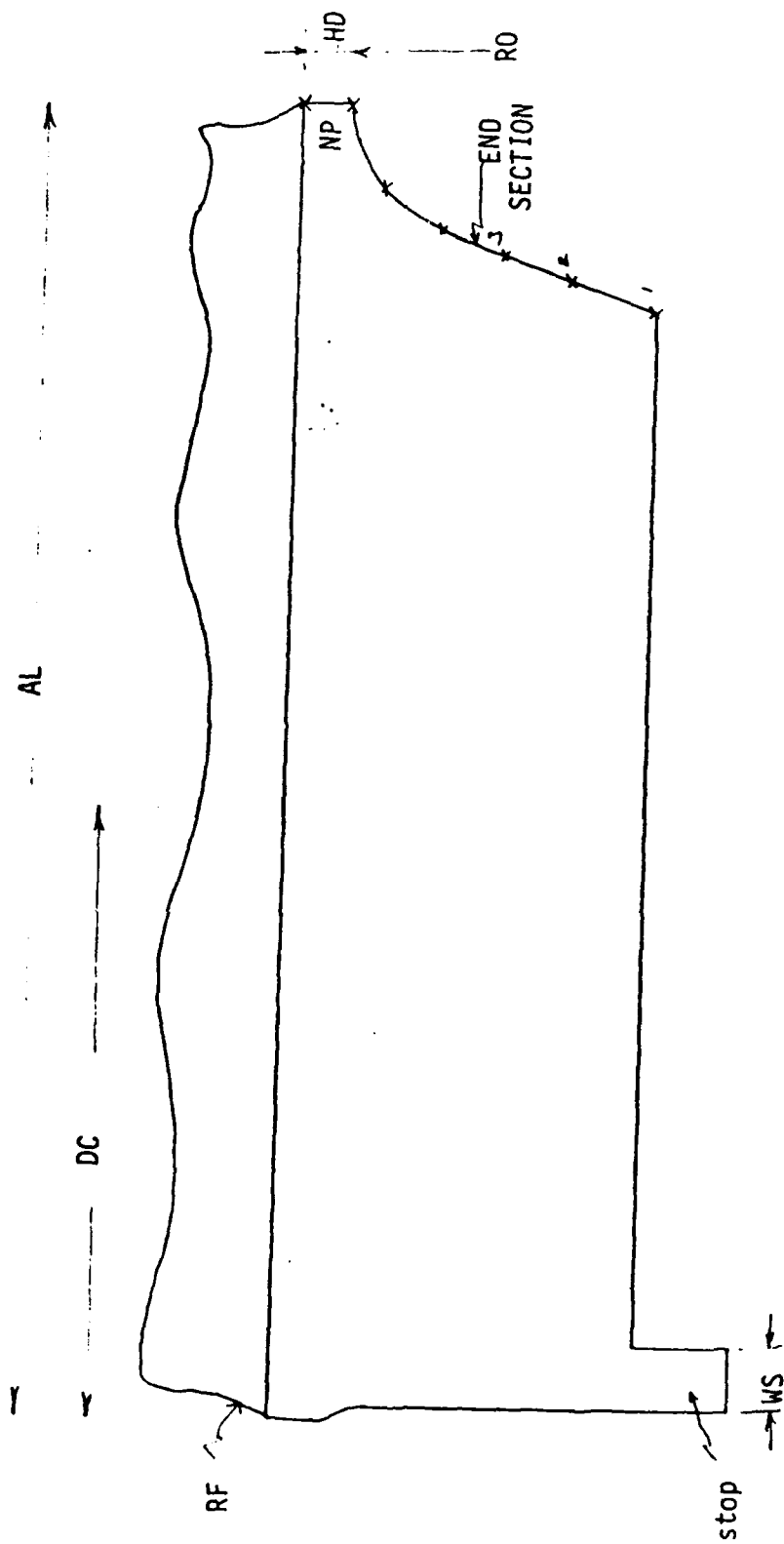


Figure 2.1.1.2: Root Side View

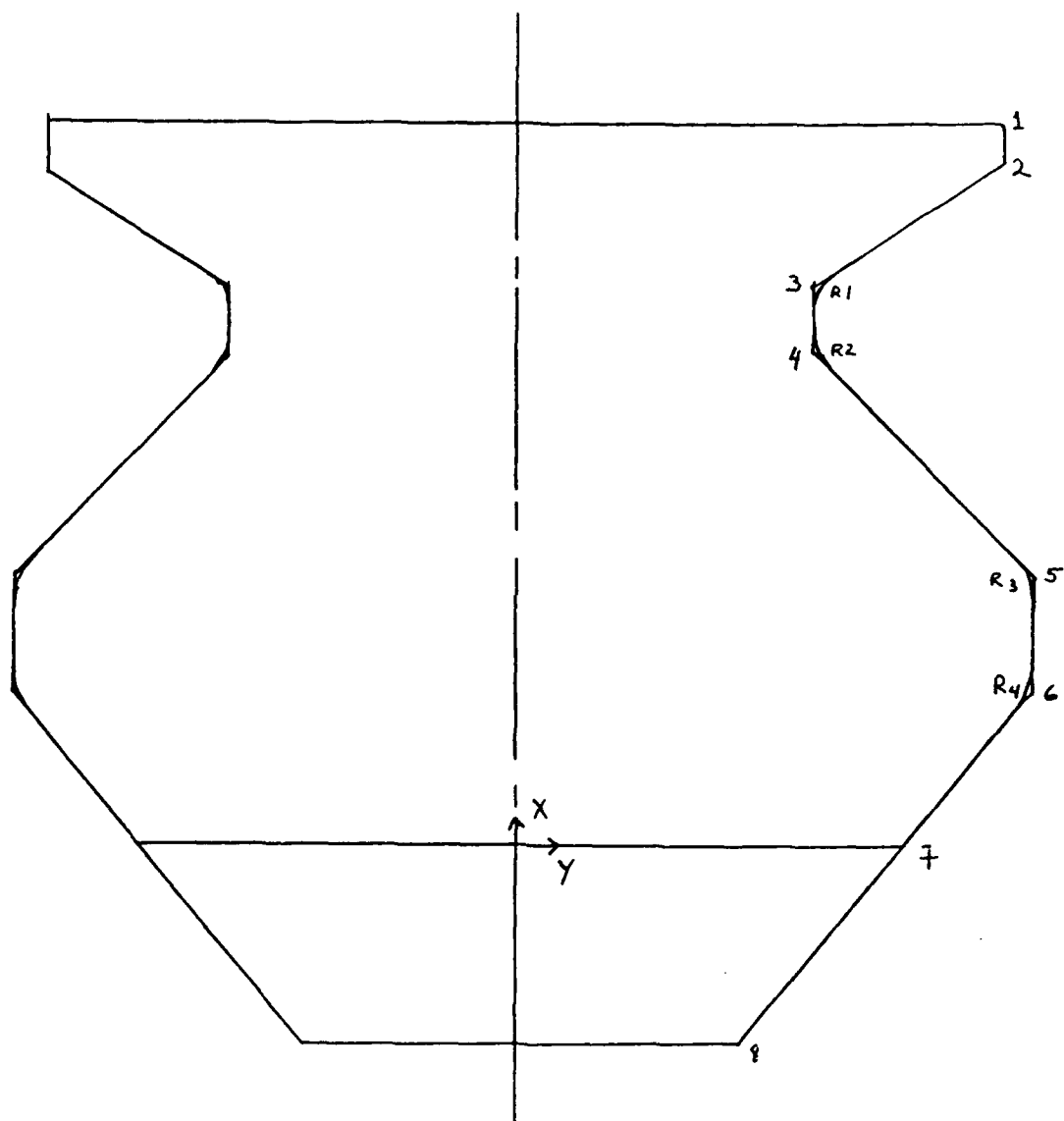


Figure 2.1.3: Root Front View

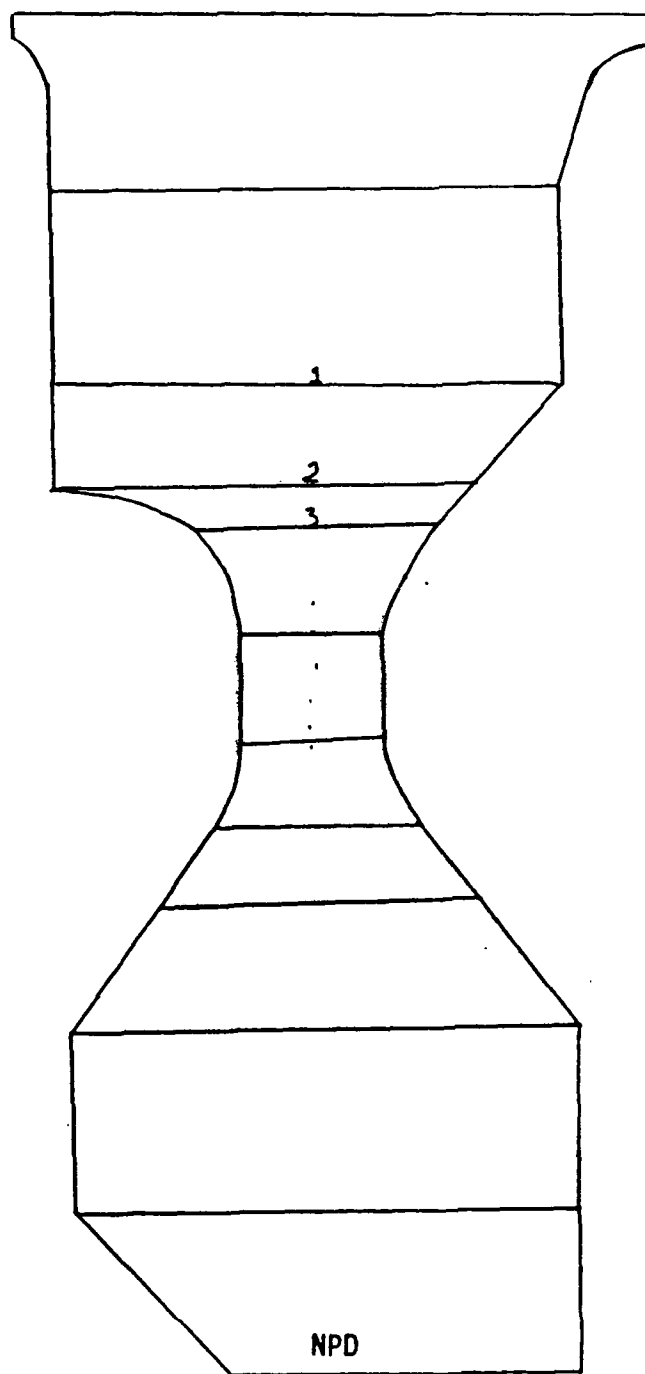


Figure 2.1.4: Disk Side View

SPEED - Rotor speed
IB - Blade of interest for back substitution

Record 9 : **FORCING** - Keyword
 C -
 A1 - If C = 0.0, tangential stream forces at hub and
 A2 Tip, respectively: otherwise, power of the
 stage and pressure drop, respectively
 A3 - If C = 0.0, axial stream forces at hub and tip,
 A4 respectively

Record 10: **EXCITATION** - Keyword
 NF - Number of frequencies to be analyzed for dynamic
 stresses
 FREQ (1) - First frequency and stimulus ratios in the
 ST(1), SA(1) Tangential and axial direction

FREQ (NF) - Last frequency and stimulus ratios
 ST (nf), SA (nf)

Record 11: **END** - Keyword

In the case of natural frequency analysis, records 9 and 10 could be eliminated. They can also be eliminated in the case of steady stress analysis under the effect of centrifugal forces only.

2.2 Example

The blade to be analyzed is the 4th compressor stage of the F100 engine. A typical airfoil profile is given in Figure 2.1.1. Root section information is presented in Figures 2.2.1 and 2.2.2. Figure 2.2.3 shows the disk data and the input file is given in Table 2.2.1.

The finite element model was generated using the preprocessor written by STI for this specific purpose. The finite element meshes for the blade as

well as for the different components are given in Figures 2.2.4 through 2.2.10. Table 2.2.2 gives the number of eight-noded isoparametric finite elements used in modeling each component.

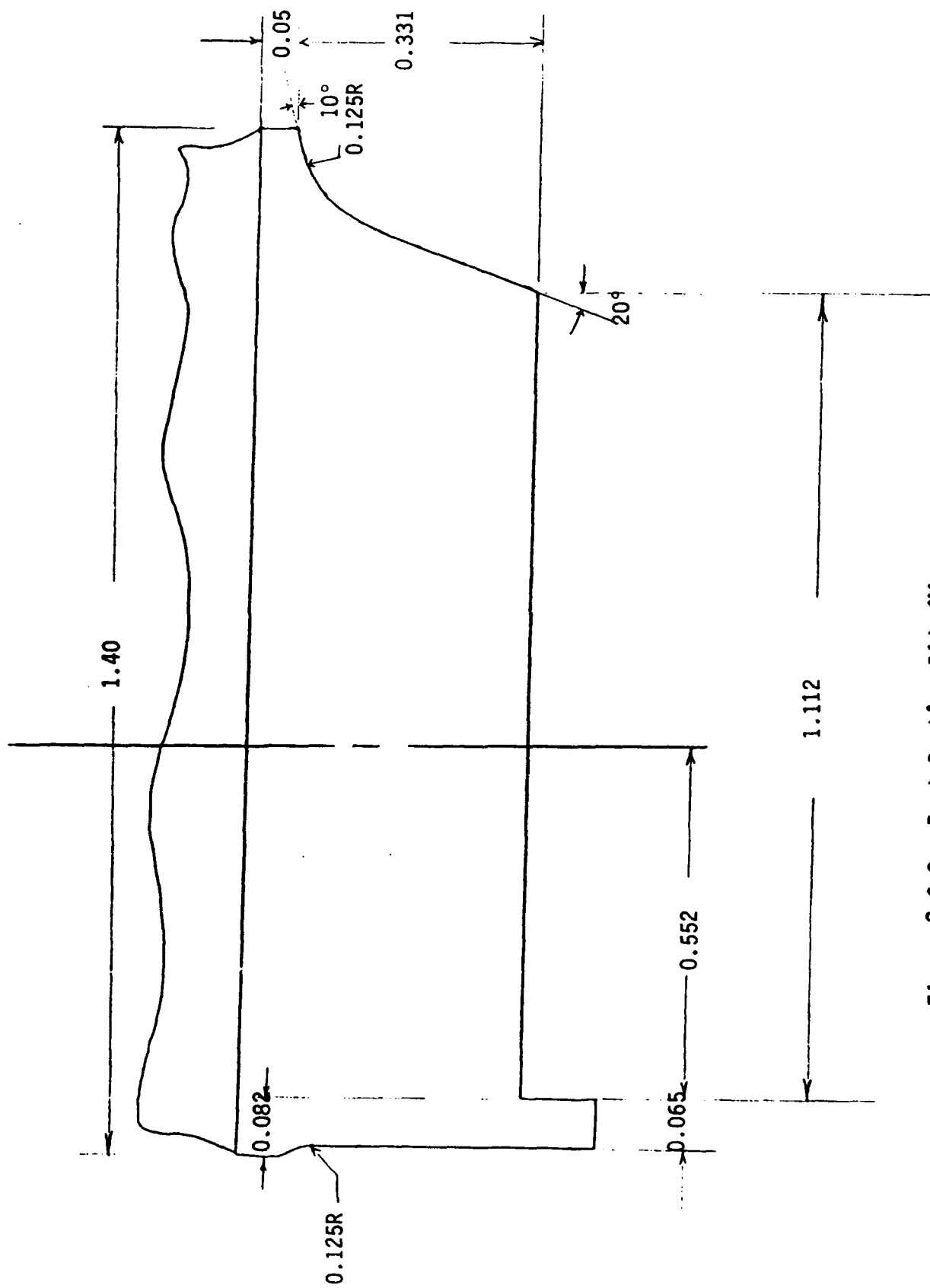


Figure 2.2.2: Root Section Side View

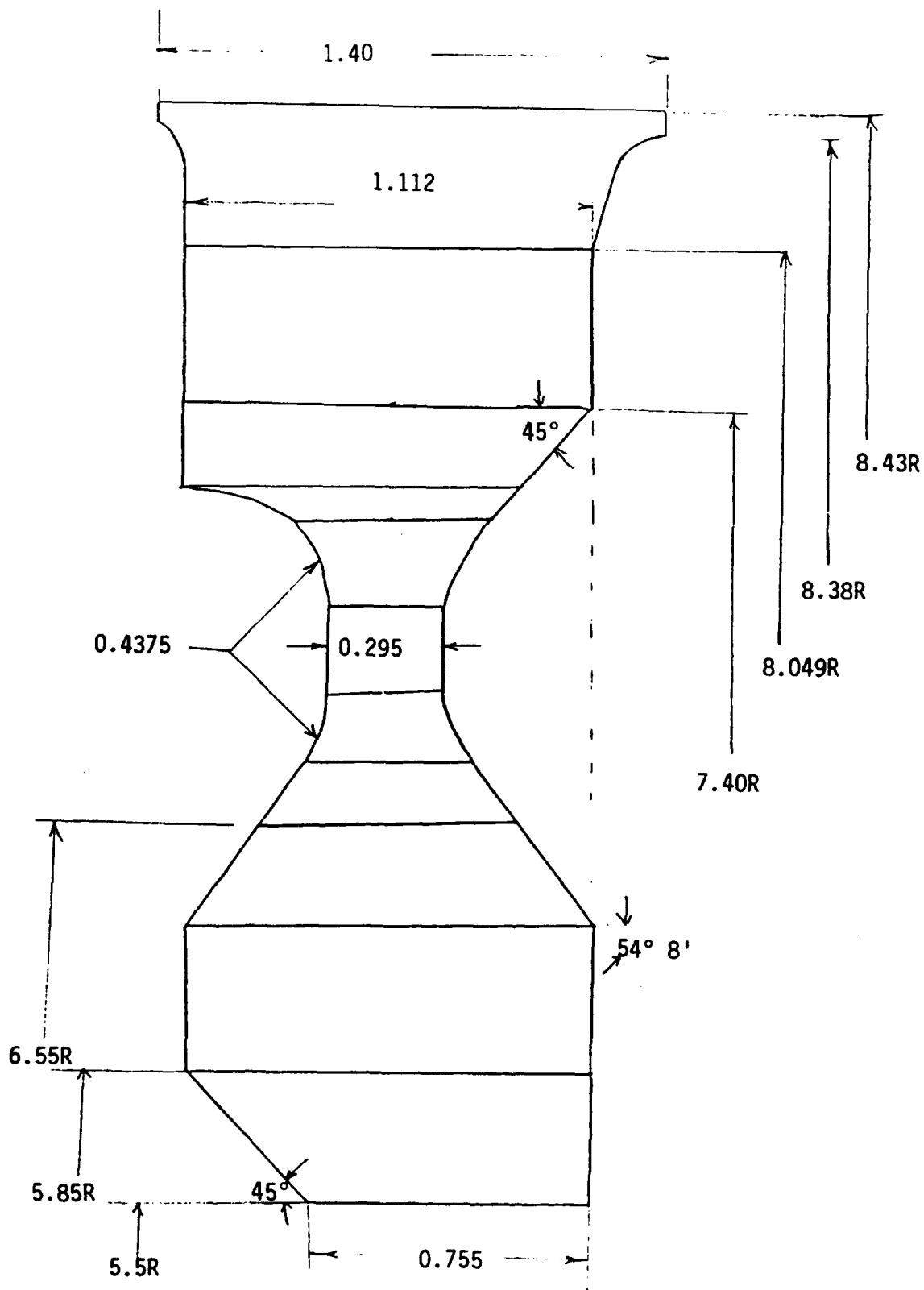


Figure 2.2.3: Disk Data

Table 2.2.1: Example Input File

AIR FORCE COMPRESSOR BLADE

COVER

0

11.639 11.729

AIRFOIL

1

11.292

-0.502 -0.394

+0.510 0.437

10

-0.500 -0.386 -0.389 -0.300 -0.286 -0.220 -0.172 -0.130

-0.072 -0.050 +0.025 0.030 +0.145 0.130 +0.264 0.230

+0.380 0.330 +0.501 0.437

10

-0.495 -0.397 -0.379 -0.330 -0.268 -0.260 -0.150 -0.180

-0.041 -0.100 +0.070 -0.010 +0.174 0.080 +0.290 0.190

+0.430 0.330 +0.509 0.430

AIRFOIL

1

10.757

-0.500 -0.445

+0.502 0.480

10

-0.499 -0.437 -0.397 -0.340 -0.292 -0.240 -0.198 -0.150

-0.112 -0.070 0.000 0.034 +0.125 0.150 +0.245 0.260

+0.366 0.370 +0.490 0.480

10

-0.491 -0.447 -0.383 -0.380 -0.268 -0.300 -0.162 -0.220

-0.052 -0.130 +0.050 -0.039 +0.163 0.070 +0.276 0.190

+0.404 0.340 +0.5025 0.469

AIRFOIL

1

10.383

-0.497 -0.479

+0.487 0.517

10

-0.496 -0.469 -0.430 -0.398 -0.300 -0.259 -0.205 -0.160

-0.118 -0.070 -0.020 0.030 +0.089 0.140 +0.210 0.260

+0.332 0.380 +0.473 0.516

10

-0.486 -0.480 -0.359 -0.400 -0.240 -0.310 -0.141 -0.230

-0.039 -0.140 +0.064 -0.040 +0.184 0.090 +0.292 0.220

+0.397 0.360 +0.488 0.500

Table 2.2.1: Example Input File (Con't)

AIRFOIL

1

9.848

-0.492 -0.524

+0.451 0.579

10

-0.490 -0.512 -0.430 -0.440 -0.330 -0.320 -0.230 -0.200

-0.130 -0.080 -0.026 0.044 +0.090 0.180 +0.220 0.330

+0.320 0.445 +0.435 0.577

10

-0.480 -0.521 -0.360 -0.449 -0.244 -0.360 -0.140 -0.270

-0.030 -0.163 +0.080 -0.041 +0.200 0.112 +0.310 0.280

+0.389 0.420 +0.456 0.563

AIRFOIL

1

9.527

-0.491 -0.546

+0.423 0.612

10

-0.491 -0.533 -0.399 -0.420 -0.301 -0.300 -0.196 -0.170

-0.091 -0.040 +0.004 0.080 +0.106 0.210 +0.206 0.340

+0.325 0.500 +0.406 0.609

10

-0.480 -0.546 -0.360 -0.470 -0.233 -0.370 -0.120 -0.260

-0.000 -0.142 +0.107 -0.010 +0.211 0.140 +0.292 0.280

+0.370 0.440 +0.429 0.596

AIRFOIL

1

9.046

-0.484 -0.568

+0.365 0.656

10

-0.484 -0.554 -0.370 -0.417 -0.291 -0.320 -0.188 -0.190

-0.093 -0.060 +0.004 0.080 +0.096 0.220 +0.183 0.360

+0.264 0.500 +0.345 0.650

10

-0.471 -0.569 -0.330 -0.480 -0.207 -0.380 -0.095 -0.270

+0.010 -0.150 +0.117 0.000 +0.208 0.160 +0.279 0.320

+0.330 0.470 +0.370 0.640

Table 2.2.1: Example Input File (Con't)

AIRFOIL

1

8.725

-0.474 -0.588

+0.291 0.695

10

-0.473 -0.571 -0.377 -0.460 -0.285 -0.350 -0.190 -0.225

-0.091 -0.080 -0.000 0.070 +0.081 0.220 +0.162 0.390

+0.233 0.540 +0.276 0.686

10

-0.460 -0.586 -0.335 -0.510 -0.210 -0.420 -0.105 -0.310

+0.011 -0.170 +0.113 -0.010 +0.194 0.160 +0.257 0.350

+0.291 0.530 +0.302 0.682

PLATFORM

1

8.372 0.050 0.050 1.402 0.2764 0.2764 0.634 0 0.172

21.0 0

ROOT

61 1

0.3925 0.2764 0.3425 0.2764 0.3030 0.1660 0.2625 0.1660

0.1595 0.2908 0.0806 0.2908 0.0000 0.2287 -0.1065 0.1226

0.0300 0.0300 0.0560 0.0560

0.0820

7

0.0000 1.1935 0.2105 1.2701 0.2268 1.2760 0.2850 1.3105

0.3000 1.3252 0.3425 1.4020 0.3925 1.4020

DISC

1 10

7.5950 0.5595 7.5950 -0.5520 7.4000 0.3574 7.4000 -0.5520

7.3292 0.2796 7.3292 -0.2980 7.1200 0.1515 7.1200 -0.1435

6.9516 0.1515 6.9516 -0.1435 6.6946 0.2351 6.6946 -0.2271

6.5500 0.3534 6.5500 -0.3320 6.2457 0.5530 6.2457 -0.5520

5.8500 0.5530 5.8500 -0.5520 5.5000 0.5530 5.5000 -0.2020

MATERIAL

1

3707

300

STAGE

52 1 0 60

0.002 6000 1

END

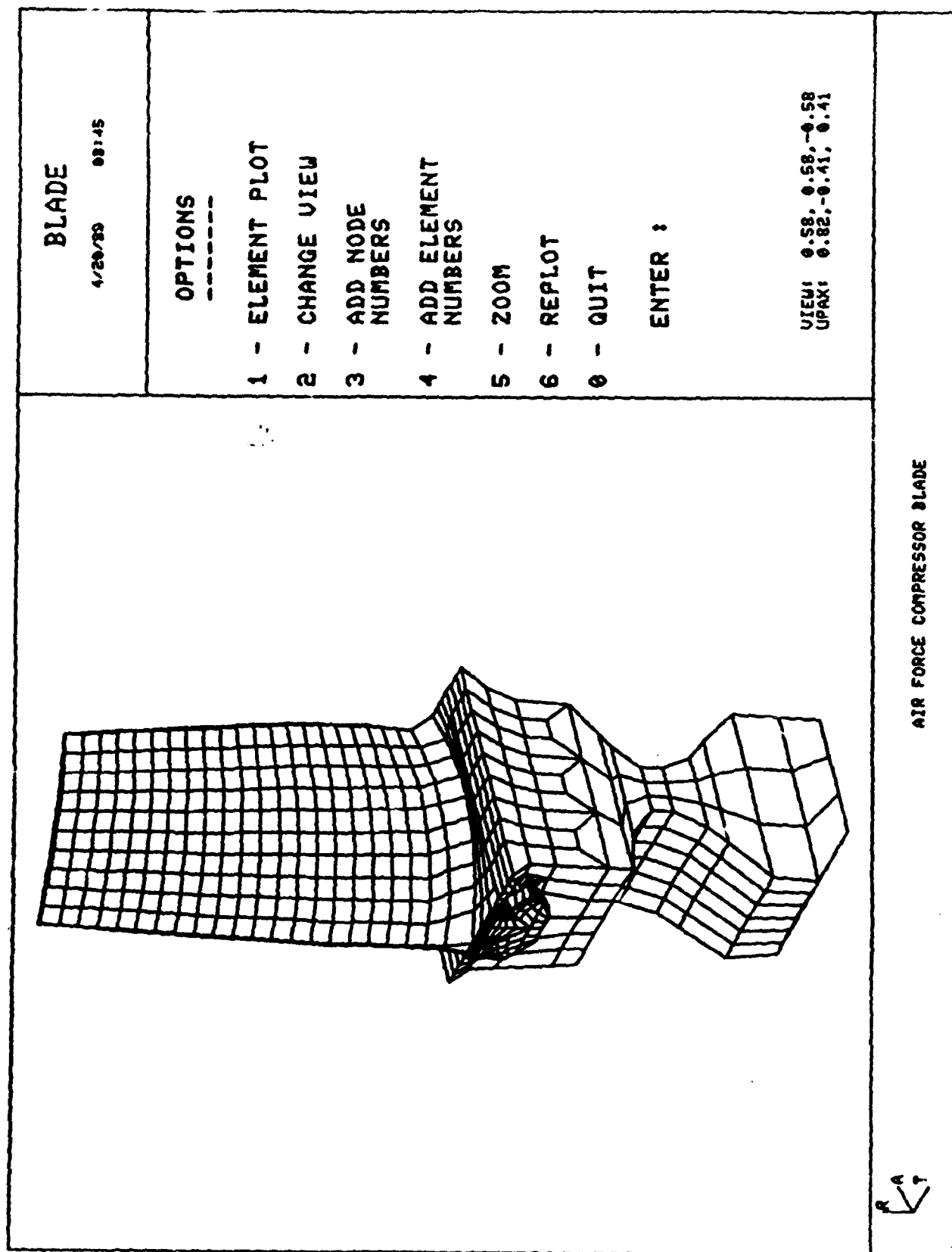


Figure 2.2.4: Example Finite Element Model

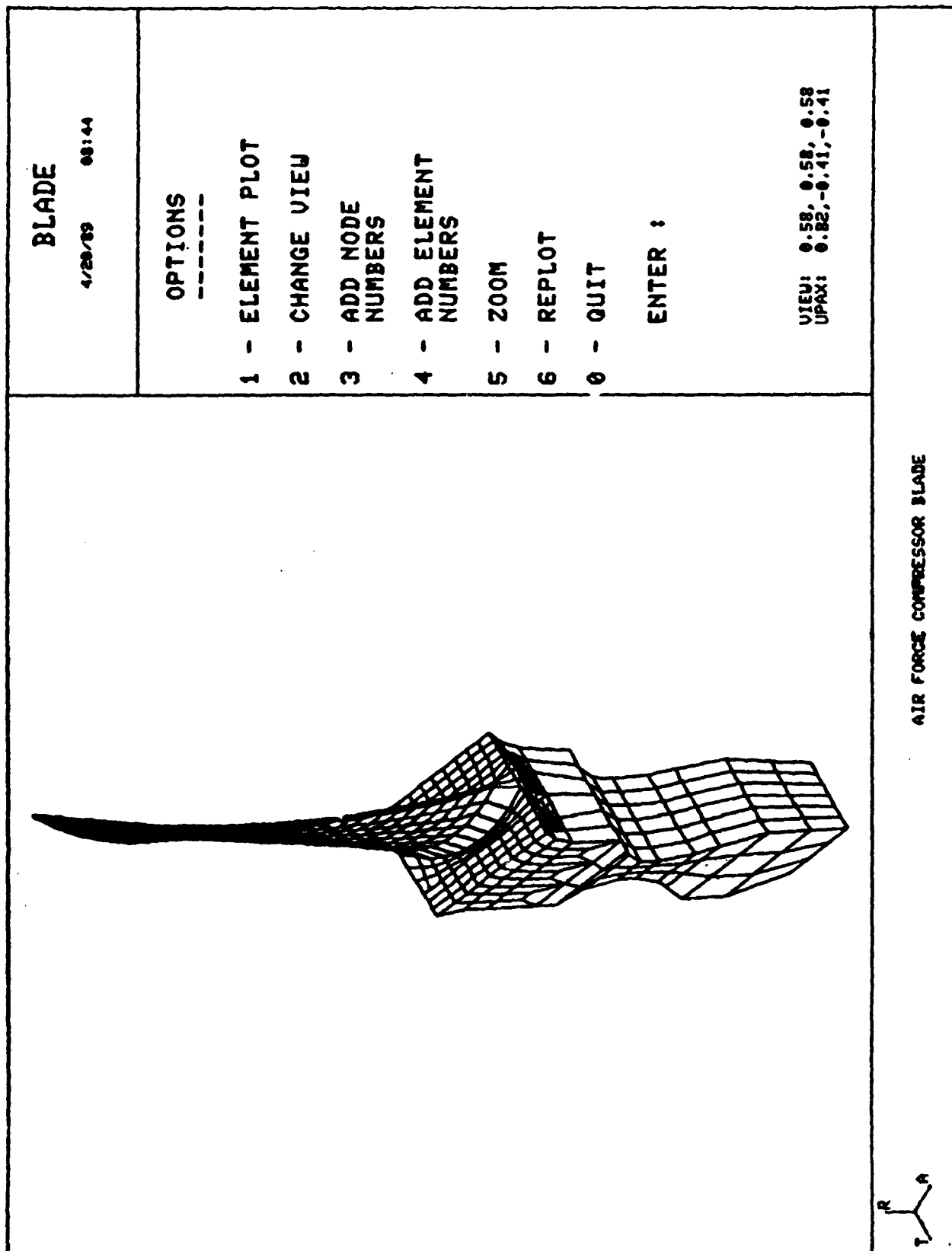


Figure 2.2.5: Finite Element Model for the Example

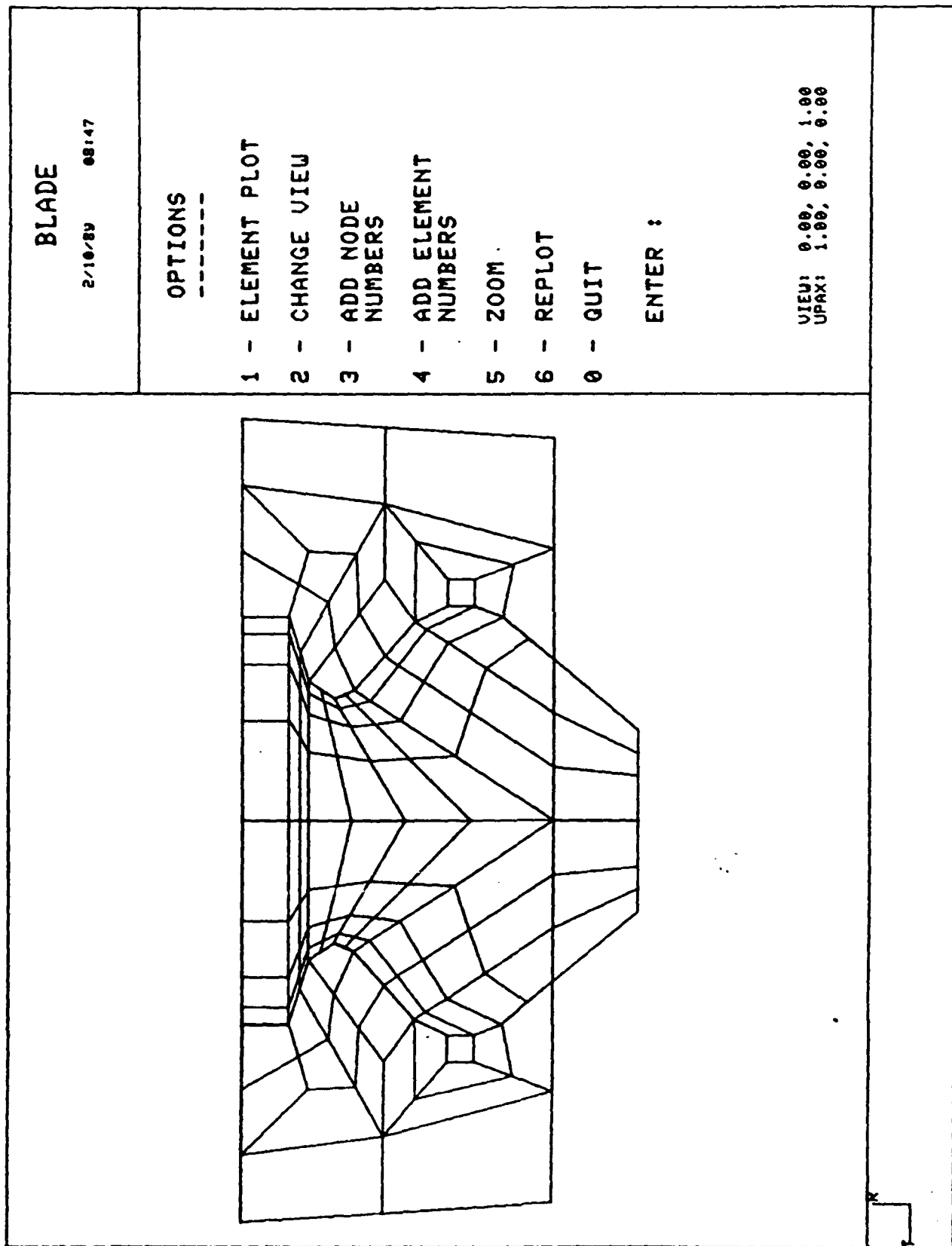


Figure 2.2.6: Finite Element Model of Root and Disk Section

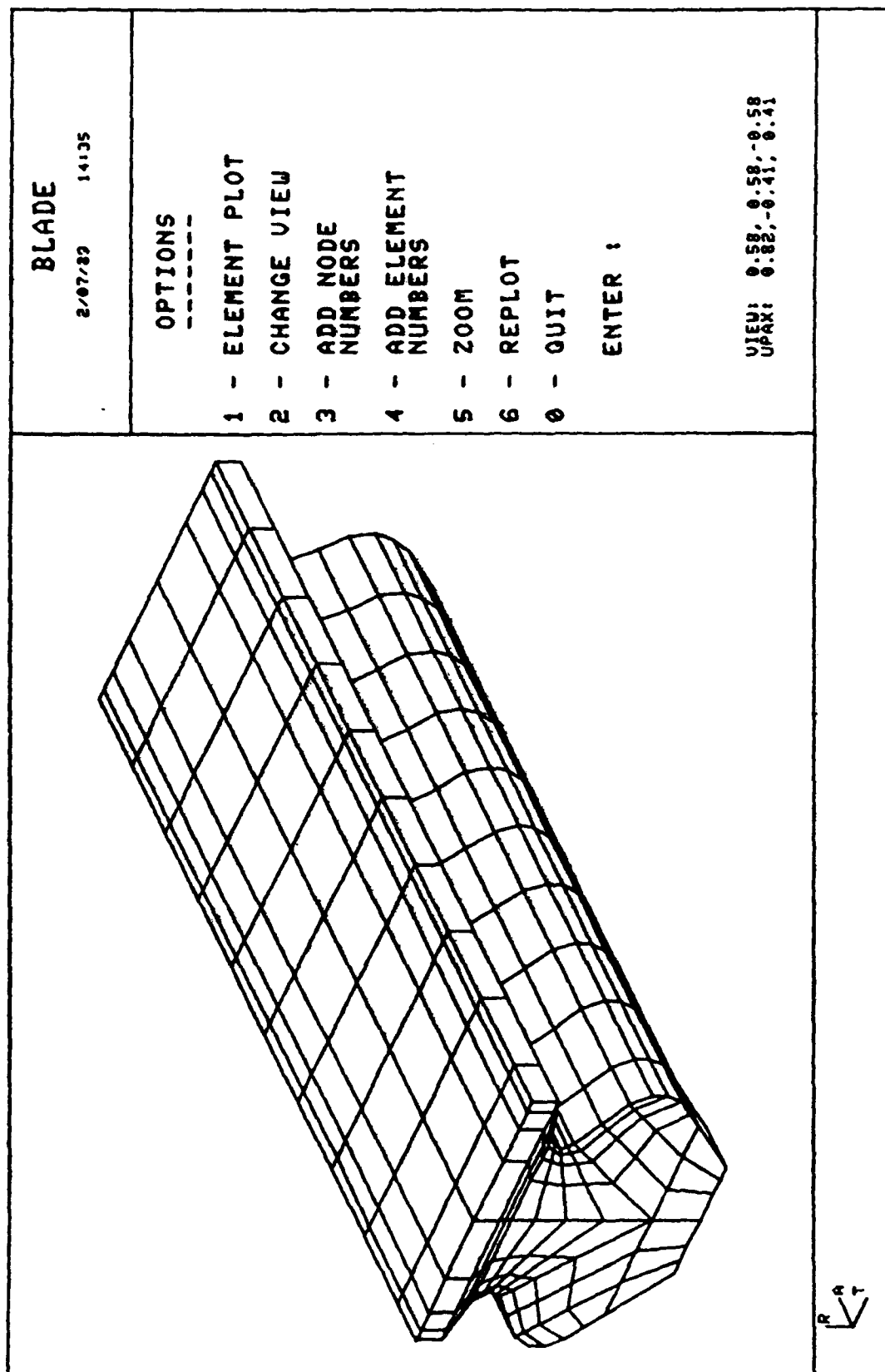


Figure 2.2.7: Finite Element Model for Root

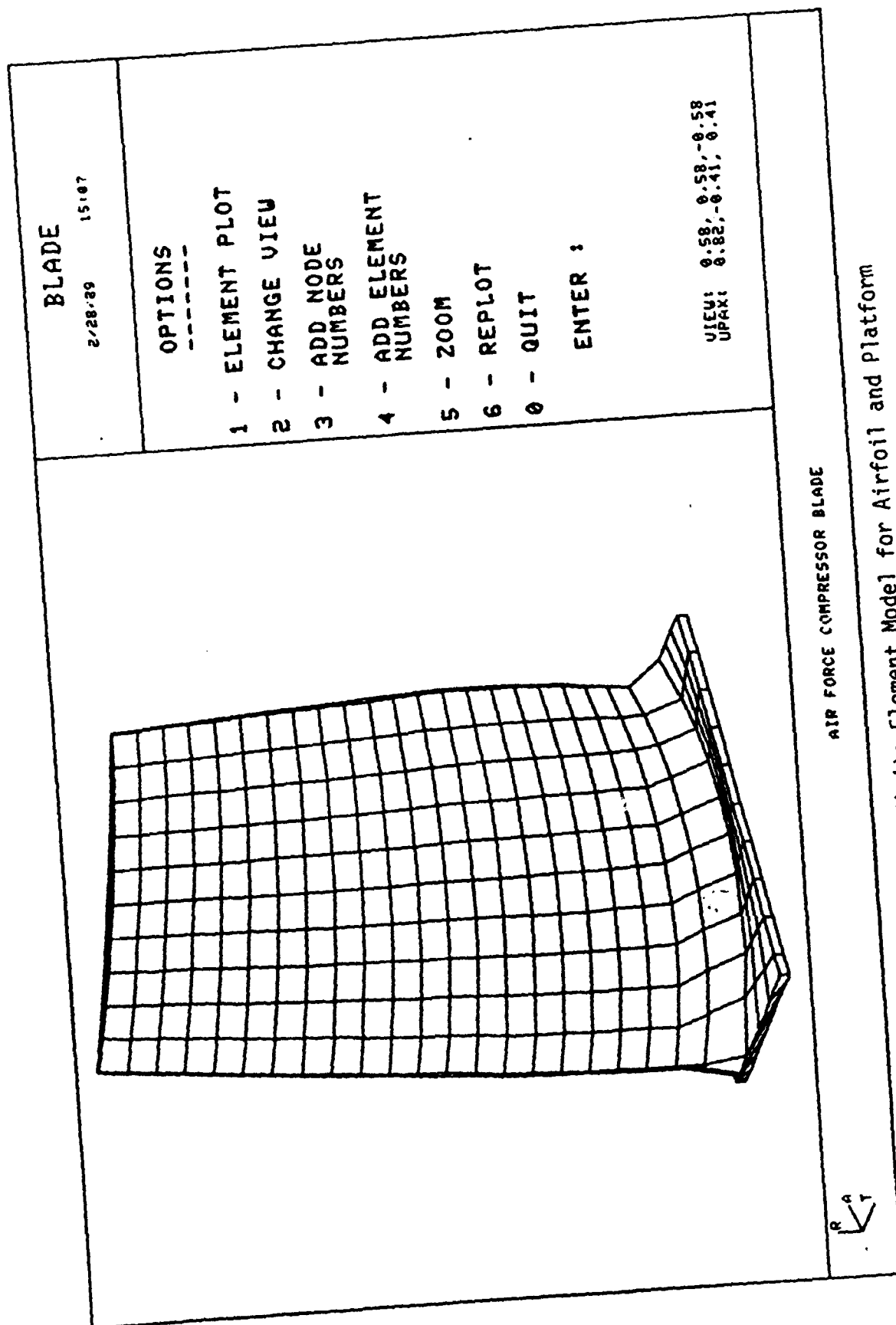


Figure 2.2.8: Finite Element Model for Airfoil and Platform

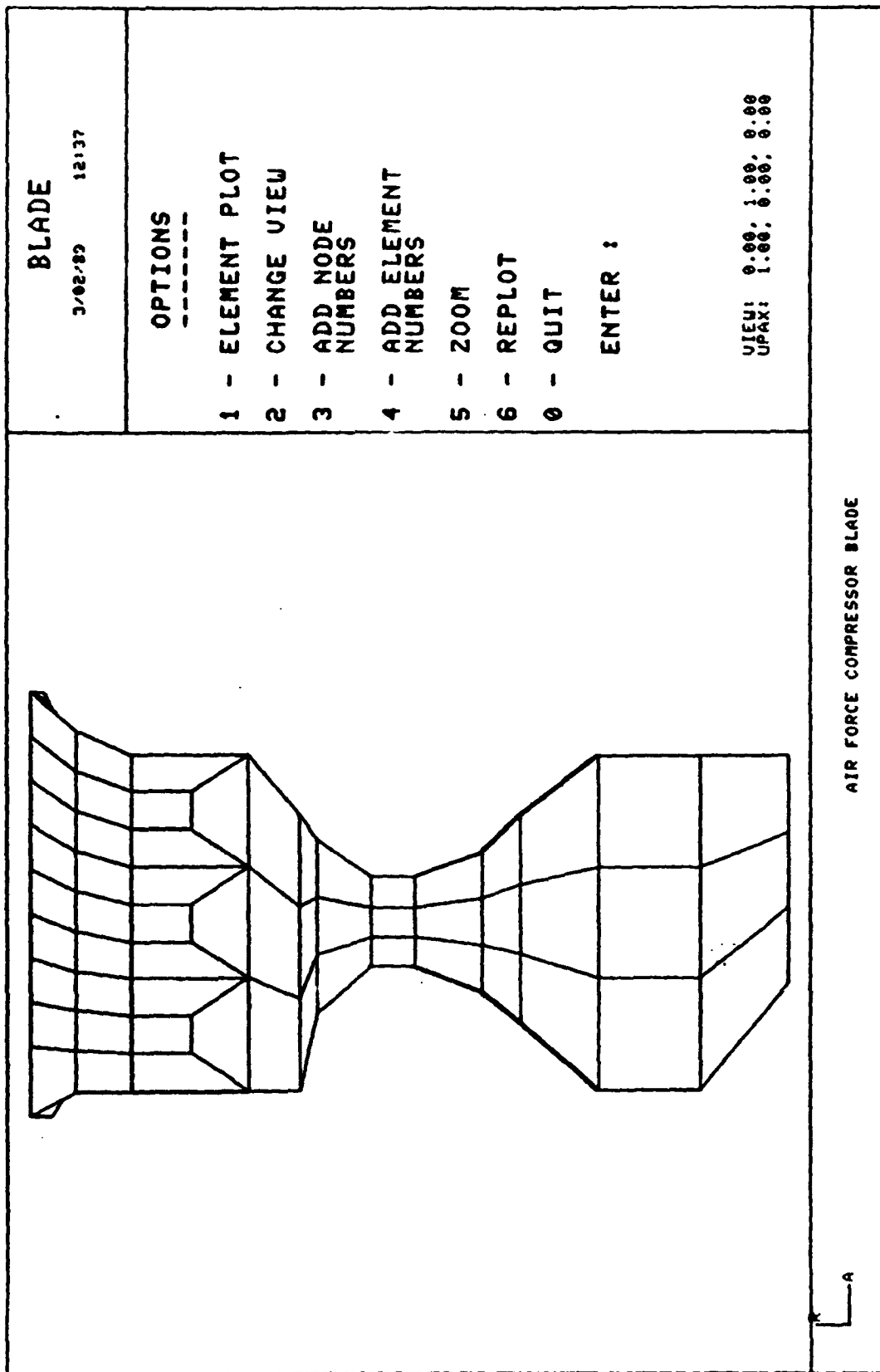


Figure 2.2.9: Finite Element Model for Disk Side View

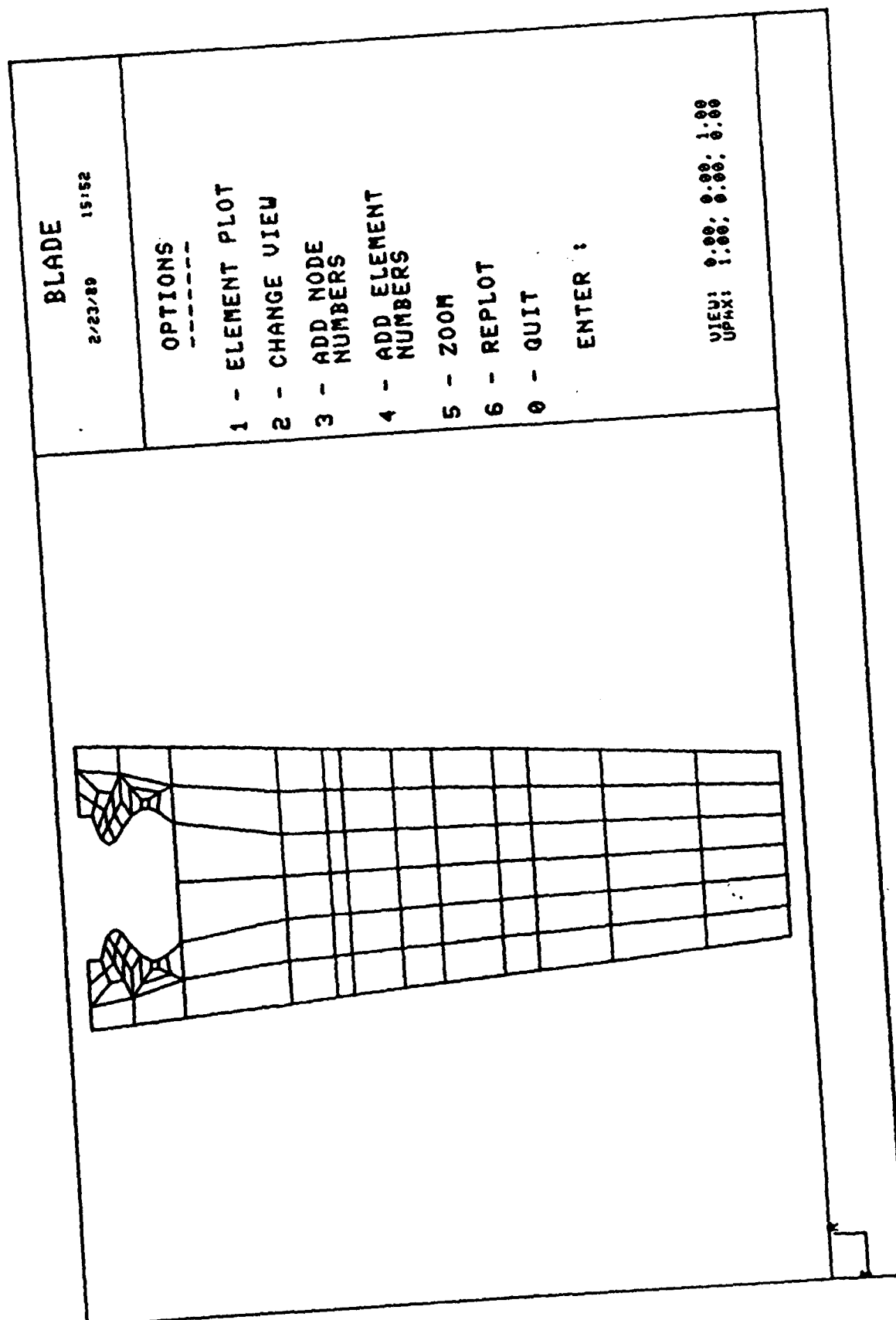


Figure 2.2.10: Finite Element Model for Disk Front View

Table 2.2.2: Details of Compressor Blade Model

Component	Number of elements
Airfoil	440
Platform	80
Root	726
Disk	594
Total	1840

3. BLADE ANALYSIS

The blade underwent two types of analysis, namely steady stress and natural frequencies analyses. Finite element programs ANSYS and BLADE were utilized to perform the computations. Both programs produced identical results which validate the BLADE program.

3.1 Steady Stress Analysis

The blade was analyzed statically under the effect of centrifugal forces. These forces result from the rotation of the rotor. A speed of 6000 rpm was used in the computation. Steady stress variations are shown in Figures 3.1.1 through 3.1.3. Maximum stress values are given in Table 3.1.1.

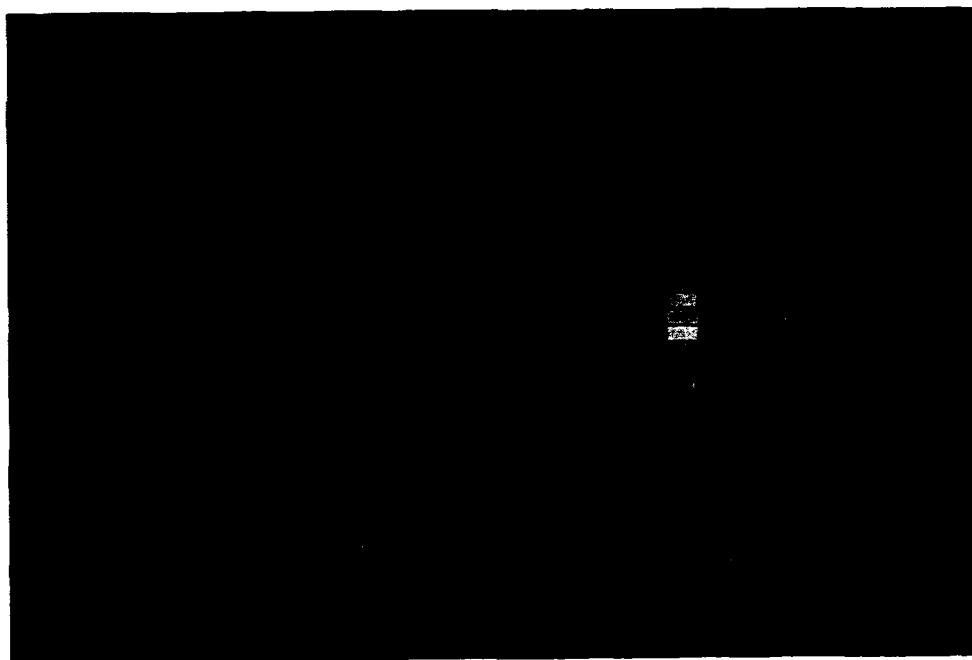


Figure 3.1.1: Maximum Nodal Steady Stresses

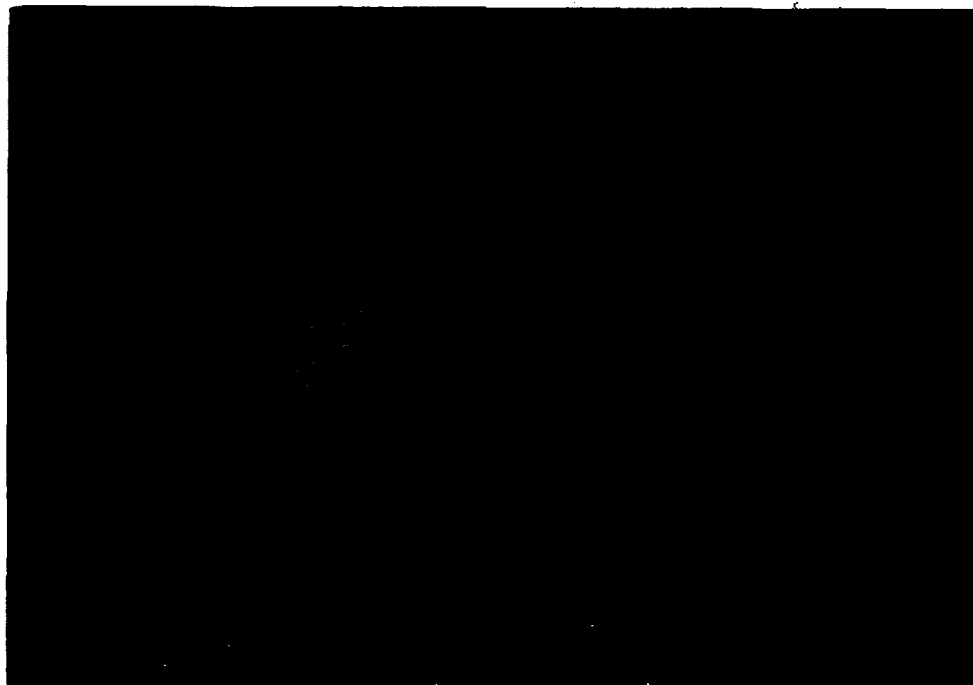


Figure 31.2: Maximum Nodal Stresses in Disk

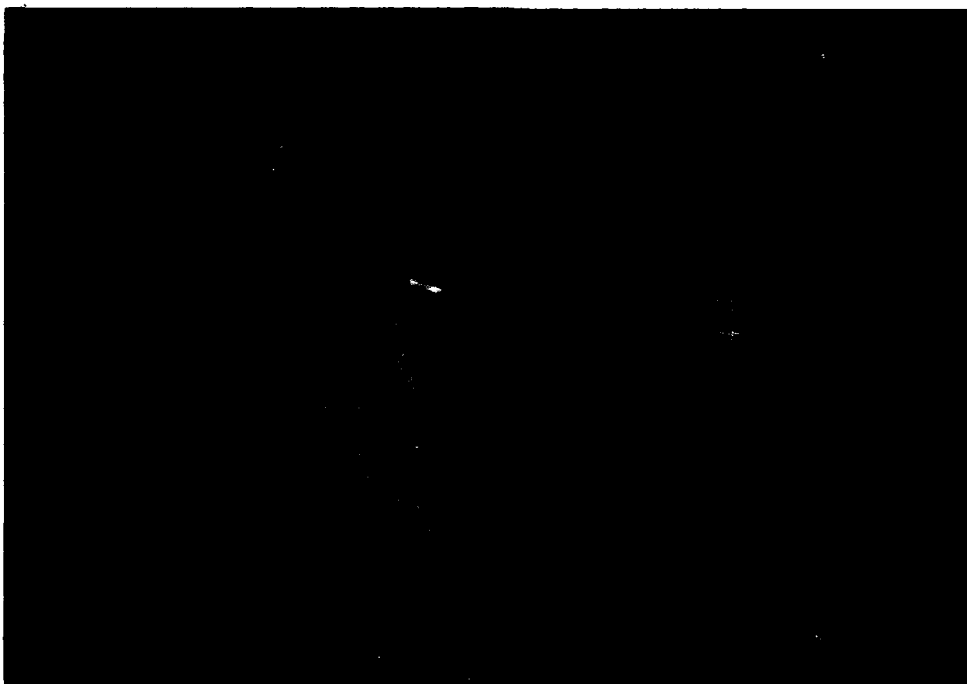


Figure 3.1.3: A Different View of Disk Nodal Stresses

Table 3.1.1 : Maximum Equivalent Stresses

<u>Element #</u>	<u>Location</u>	<u>Stresses, psi</u>	
		BLADE	ANSYS
1358	Disk	10085	10085
1359	Disk	8604.5	8604.5
1546	Disk	8460.0	8460.0
1361	Disk	8411.1	8411.1
1362	Disk	8375.8	8375.8
1360	Disk	8315.4	8315.4

Maximum equivalent stress in:

	<u>BLADE</u>	<u>ANSYS</u>
Airfoil	4364.9 psi	4364.9 psi
Platform	2530.9 psi	2530.9 psi
Root	7569.0 psi	7569.0 psi

3.2 Natural Frequency Analysis

Natural Frequency Analysis was performed on the blade model. The equation of motion for free vibration is of the eigenvalue type,

$$[M]\{\ddot{X}\} + [K]\{X\} = 0$$

where $[M]$ and $[K]$ are the mass and stiffness matrices and $\{X\}$ is the displacement vector. By solving this eigenvalue problem, the eigenvectors are the mode shapes while the eigenvalues yield the natural frequencies. Due to the large number of degrees of freedom describing the model, Guyan reduction technique was implemented. At operation speed, centrifugal stresses stiffen the blade and therefore the natural frequencies at speed become higher than their corresponding values at zero rpm. The frequency values at speed and at zero rpm are given in Table 3.2.1. Mode shapes are presented in Figures 3.2.1 through 3.2.5. A Campbell diagram which shows the effect of speed on the values of the natural frequencies is given in Figure 3.2.6.

Table 3.2.1 : Natural Frequencies for a Single Blade

Mode #	Frequency (hz)		
	ANSYS at 0 rpm	BLADE at 0 rpm	at 6000 rpm
1	611.0	611.0	657.6
2	2173.8	2173.8	2212.8
3	2610.6	2610.6	2625.8
4	2854.3	2854.8	2866.6
5	4939.8	4939.8	4969.9
6	5466.2	5466.2	5502.3
7	8565.8	8565.8	8597.4
8	9313.4	9313.4	9347.1
9	10247.0	10247.0	10257.6
10	11118.0	11118.0	11141.9
11	12865.0	12865.0	12902.0

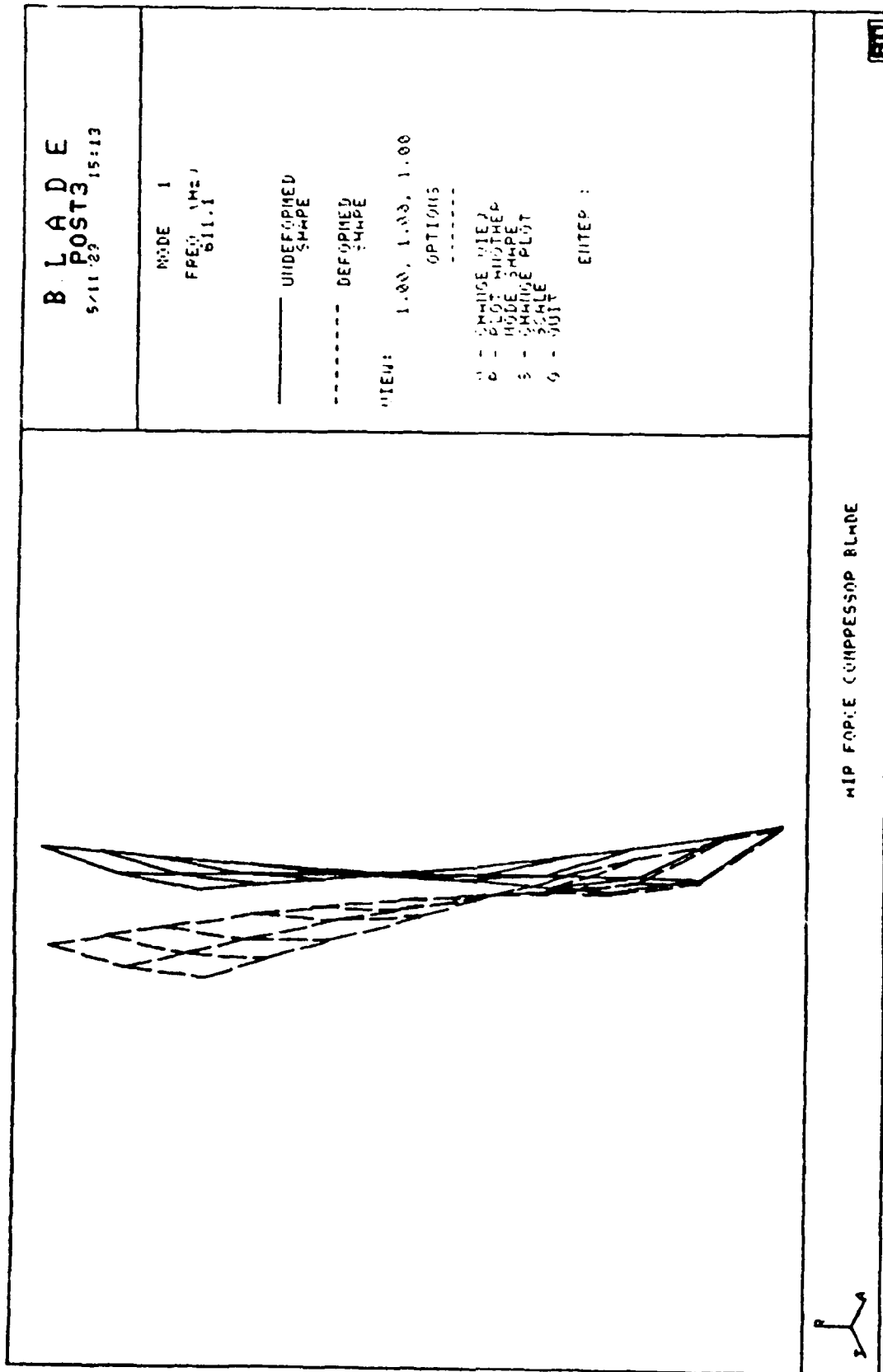


Figure 3.2.1: Mode Shape 1

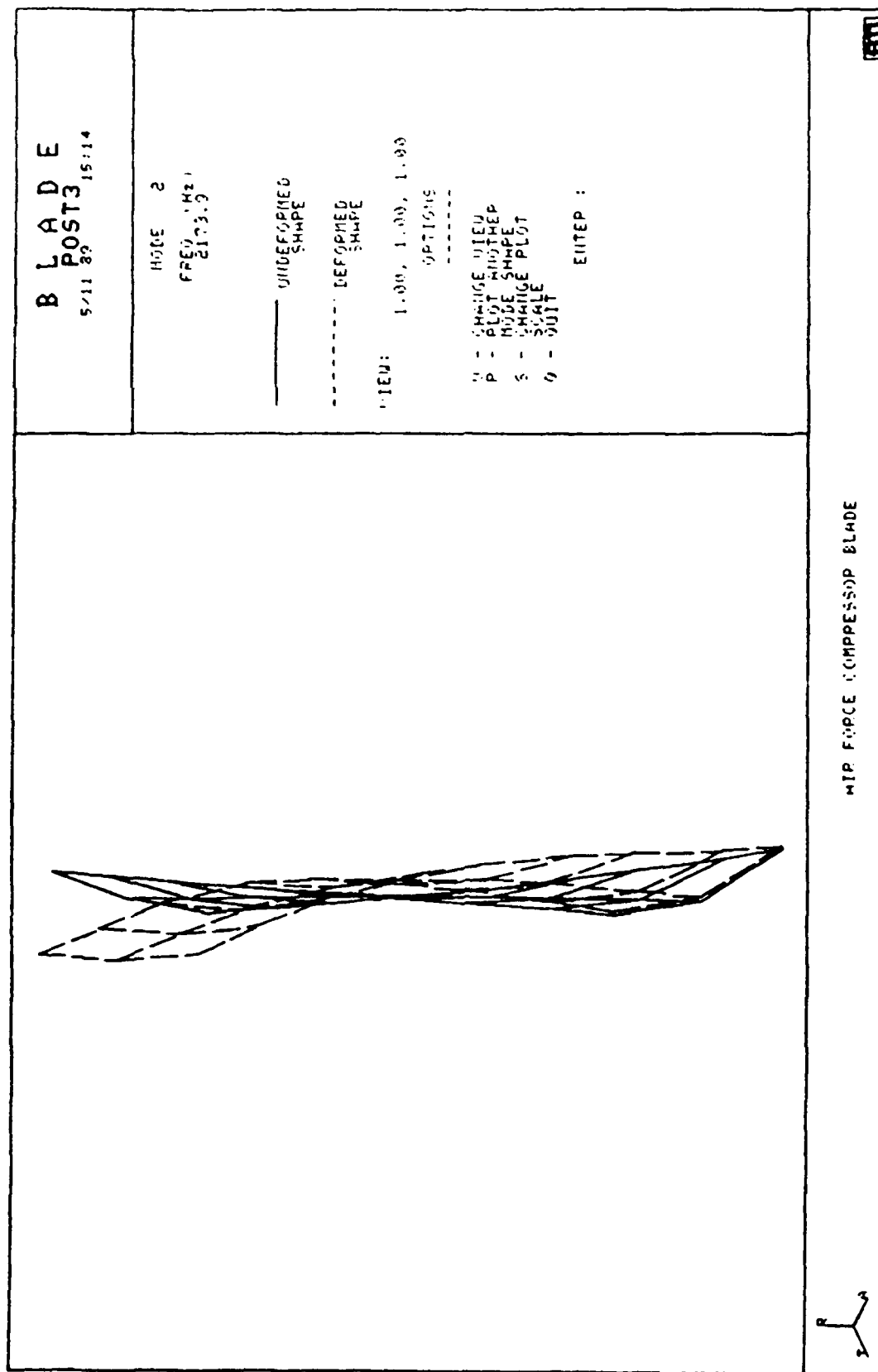


Figure 3.2.2: Mode Shape 2

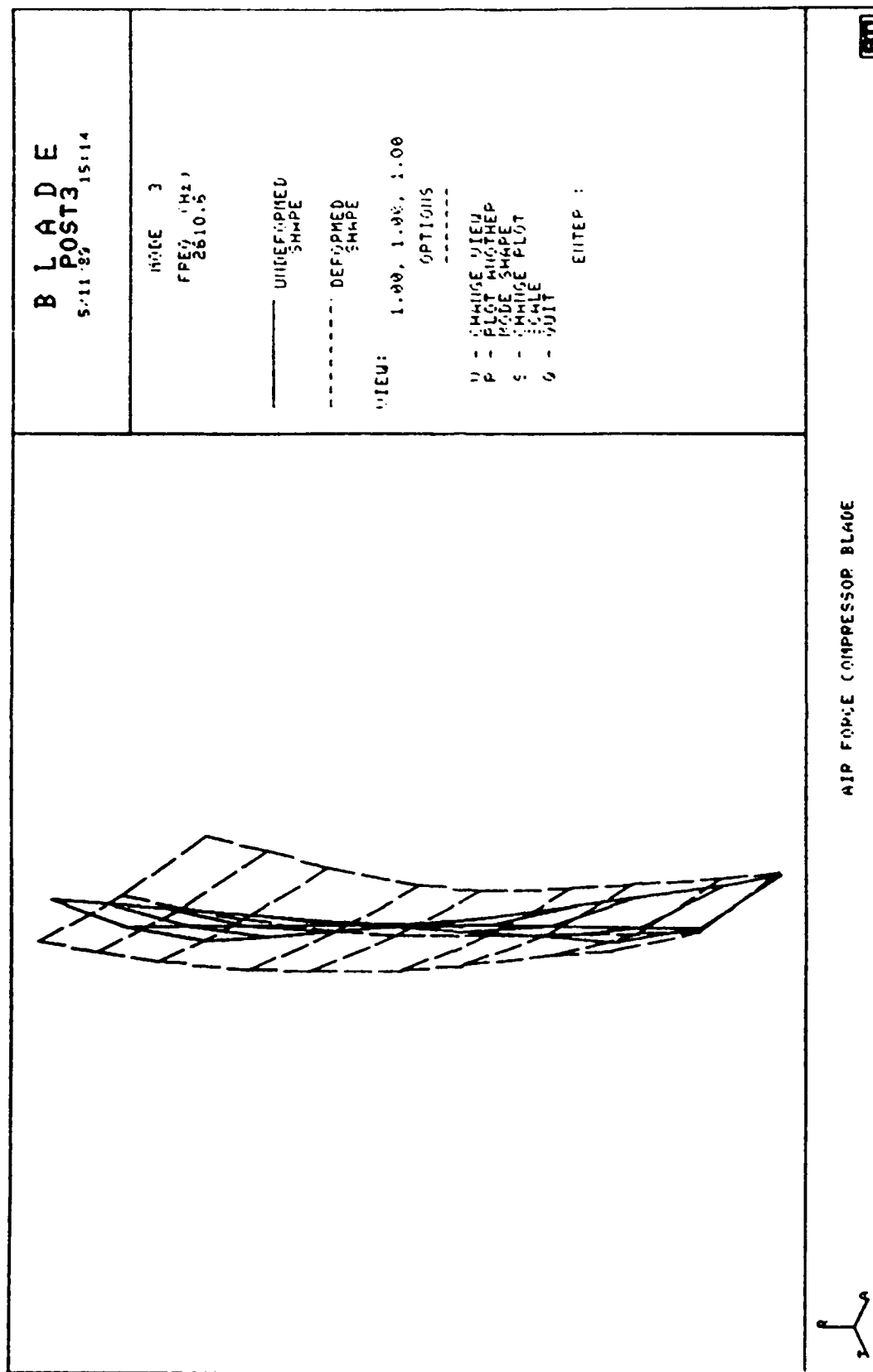


Figure 3.2.3: Mode Shape 3

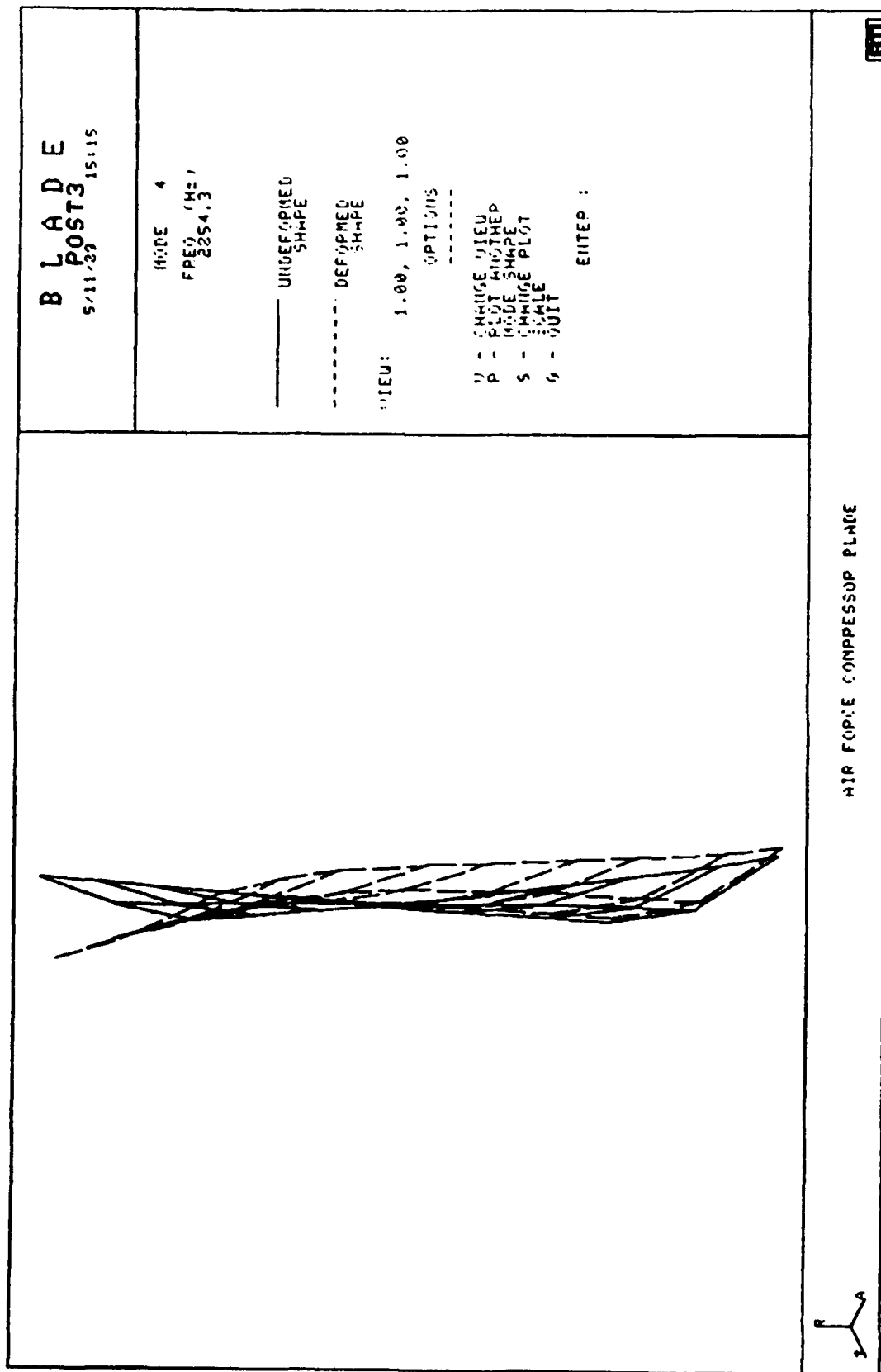


Figure 3.2.5: Mode Shape 4

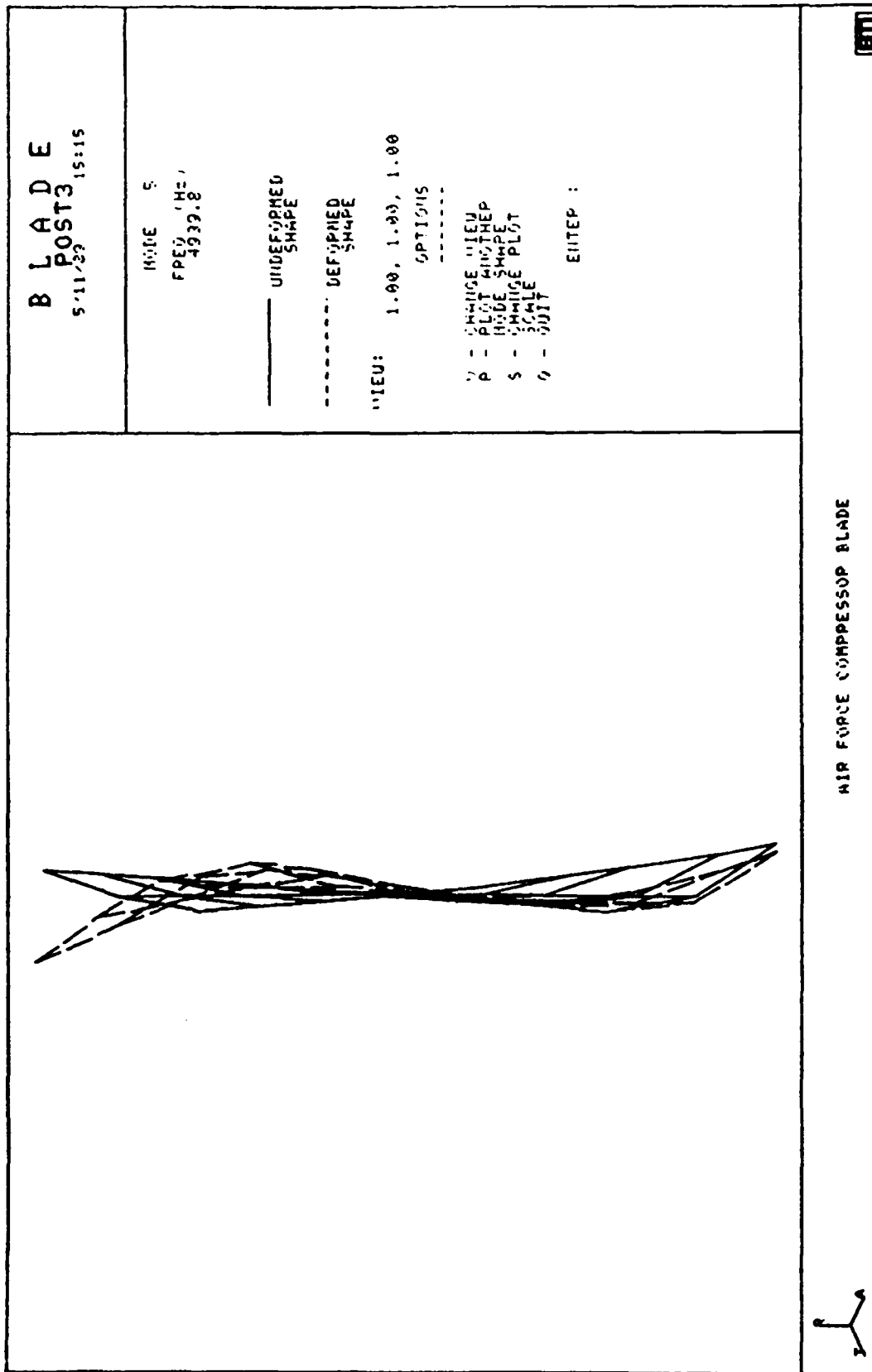


Figure 3.2.5: Mode Shape 5

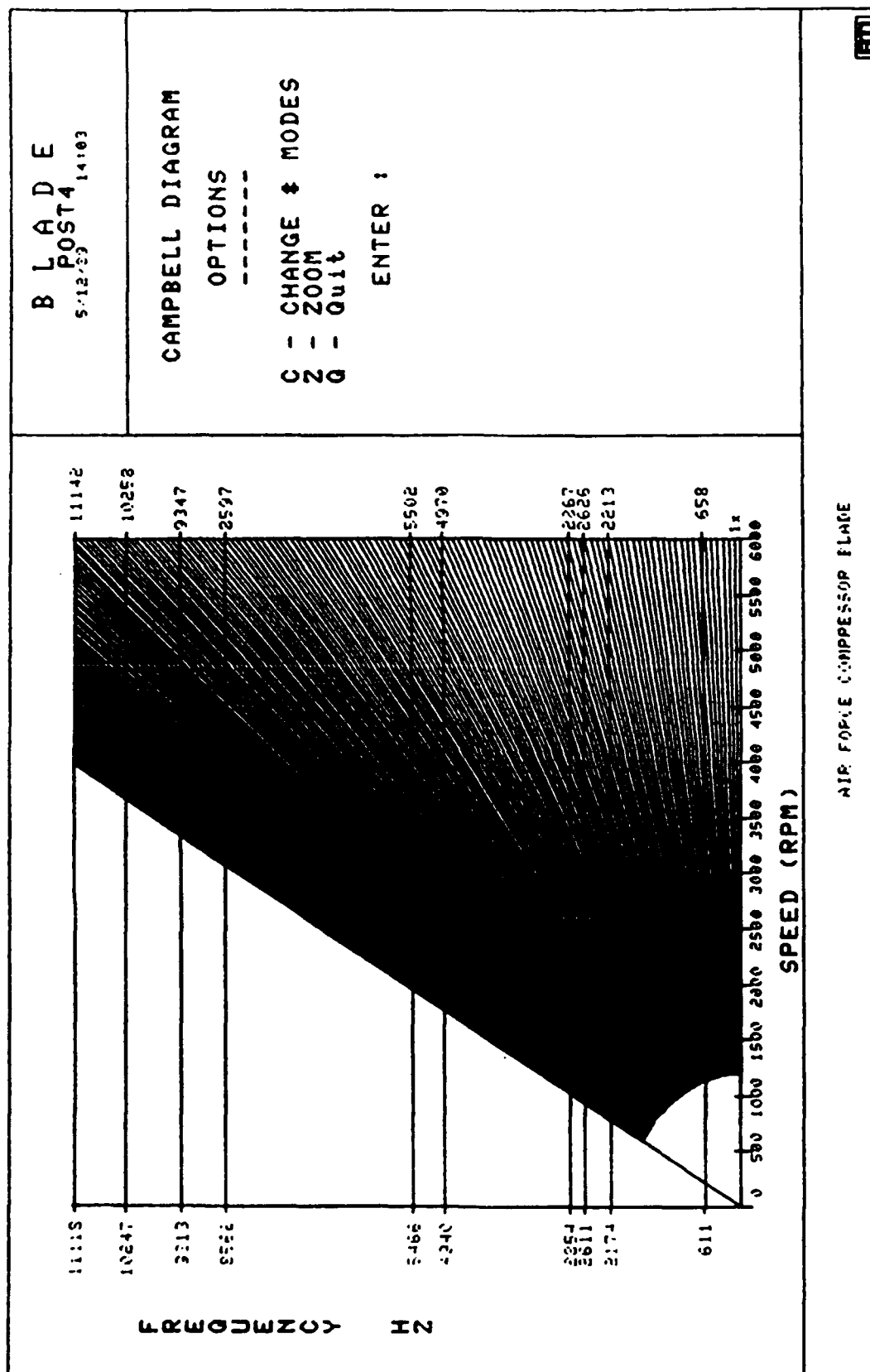


Figure 3.2.6: Campbell Diagram

3.3 Comparison with Test Results

Test results for natural frequencies test data were provided by AFWAL in the form of Holographic photos. The BLADE program was utilized to plot the displacement contours for the different mode shapes. Comparison of the calculated natural frequencies to the test data is given in Table 3.3.1. For Titanium material, it is known that the elastic modulus is strongly dependent on the thermal-mechanical processing. For bar stock, elastic modulus is about 16×10^6 psi. For forged blade vane, the modulus of elasticity could become 18.0×10^6 psi. As a result, the blade natural frequency can vary as much as 5 percent. As a matter of fact, the modulus for Titanium changes for one blade from one component to the next as shown in Table 3.3.2 obtained from tests conducted by Westinghouse. The analysis was carried out using a modulus of 17.0×10^6 psi as shown in Table 3.3.1 in column (2). They compare favorably with the test data as shown by the percentage deviation in column (3). The table also shows that mode 4, 7, and 9 were missing from the experimental data. The Holograms are next compared to the calculated displacement contours in Figures 3.3.1 through Figures 3.3.8.

**Table 3.3.1: Comparison of Calculated Frequencies
and Test Data**

Test Frequency hz	Calculated Frequency hz	% Deviation
602	611.0	+1.5
2138	2173.8	+1.67
2701	2610.6	-3.35
missed	2854.3	---
5200	4939.8	-5.0
5536	5466.2	-1.26
missed	8565.8	---
9480	9313.4	-1.76
missed	10247.0	---
10800	11118.0	+2.90
12620	12865.0	+1.94

Table 3.3.2: Dynamic Modulus of Prototype
TI-6AL-4V Blades

<u>Row Number</u>	<u>Location</u>	<u>Direction</u>	<u>Average Dynamic Tensile Modulus (ksi)</u>
1	Airfoil	long	17.61
1	Root	long	17.33
1	Root	trans.	18.10
2	Airfoil	long	17.38
2	Airfoil	trans.	17.71
2	Root	trans.	17.97

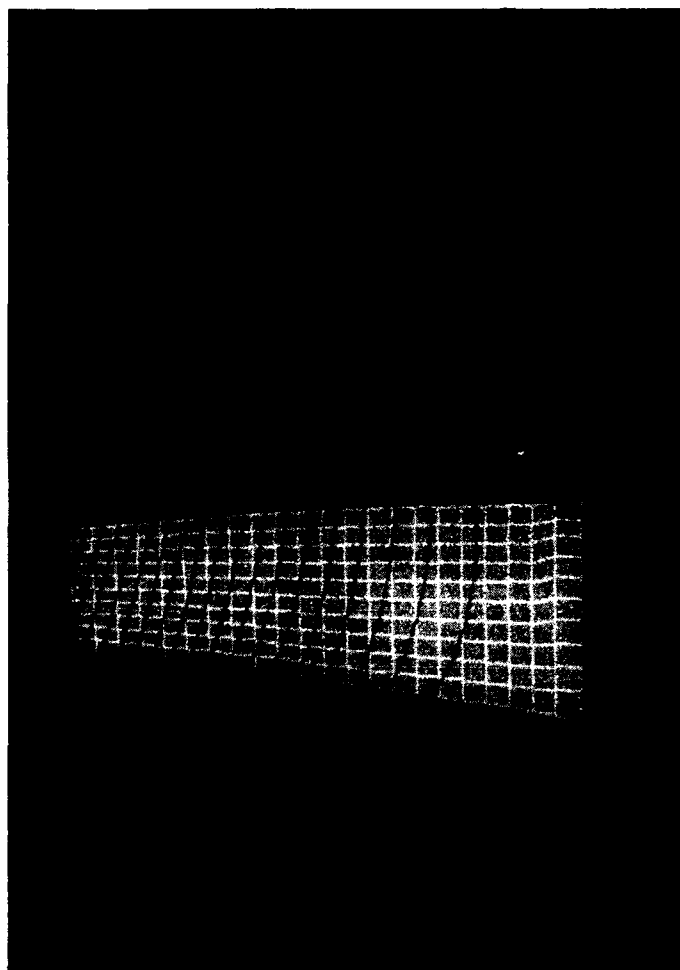
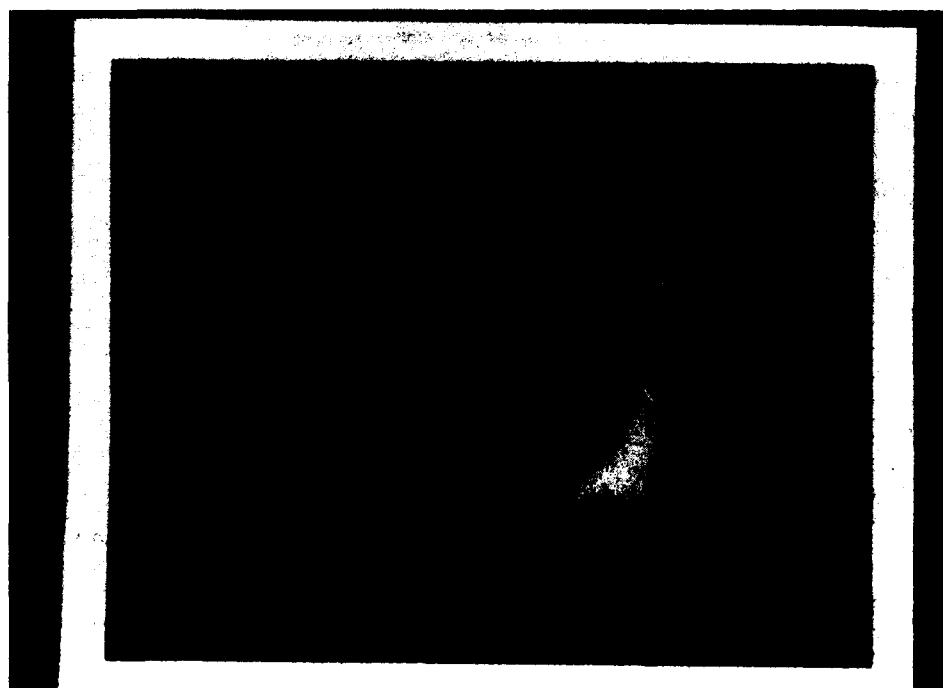


Figure 3.3.1: Comparison of Test Holograms and Analytical Results for Mode 1

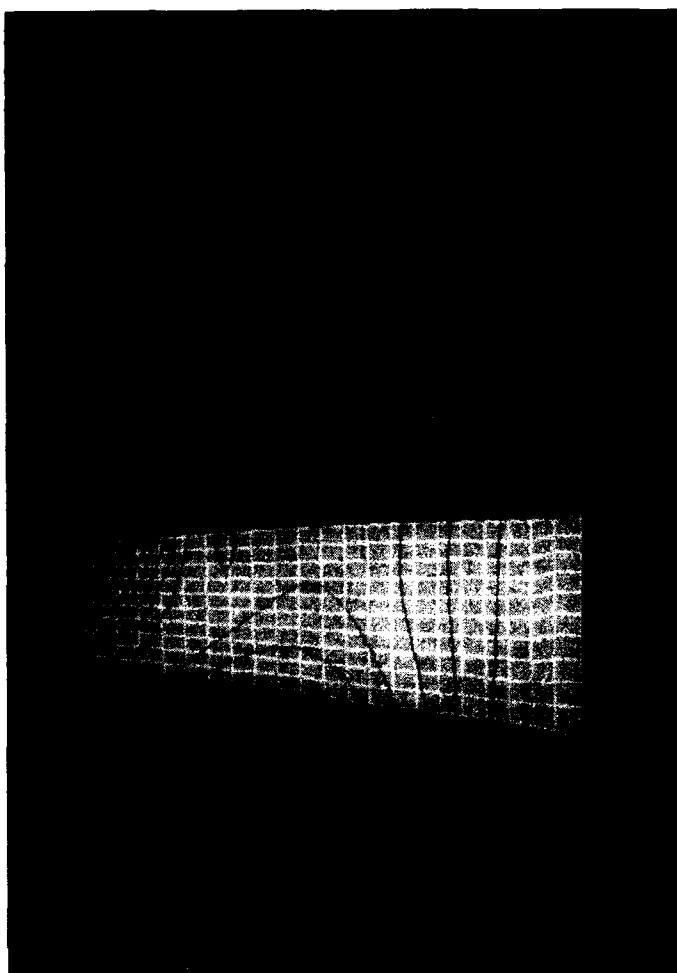
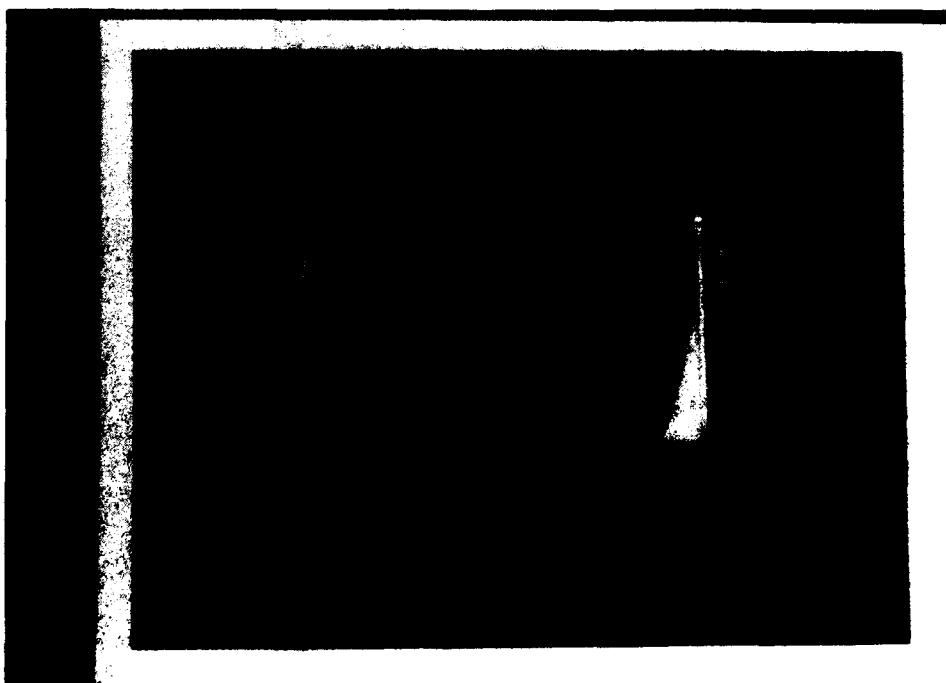


Figure 3.3.2: Comparison of Test Holograms and Analytical Results for Mode 2

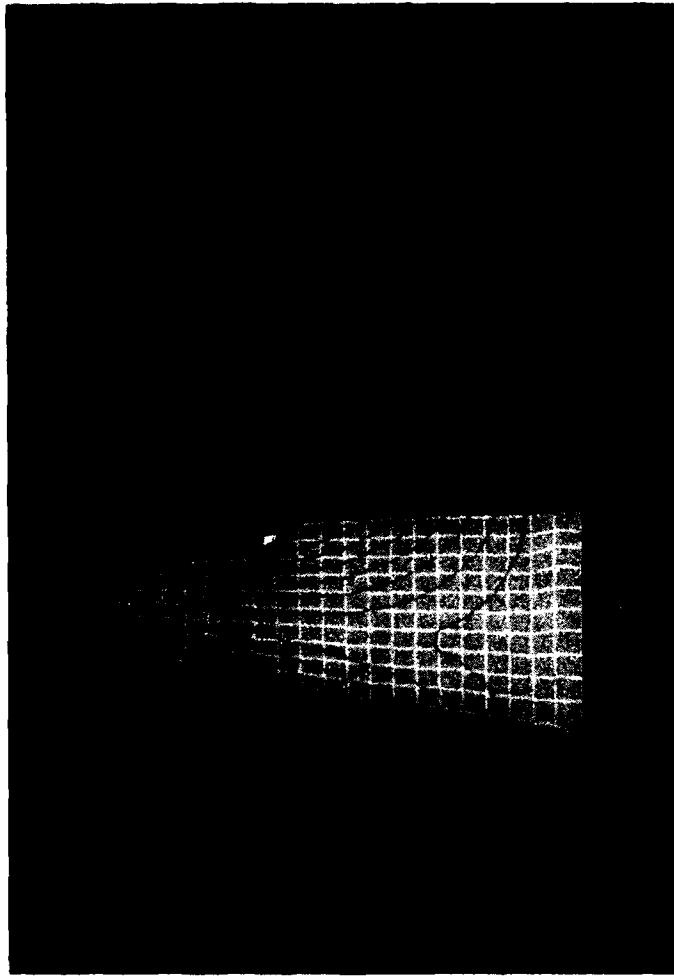
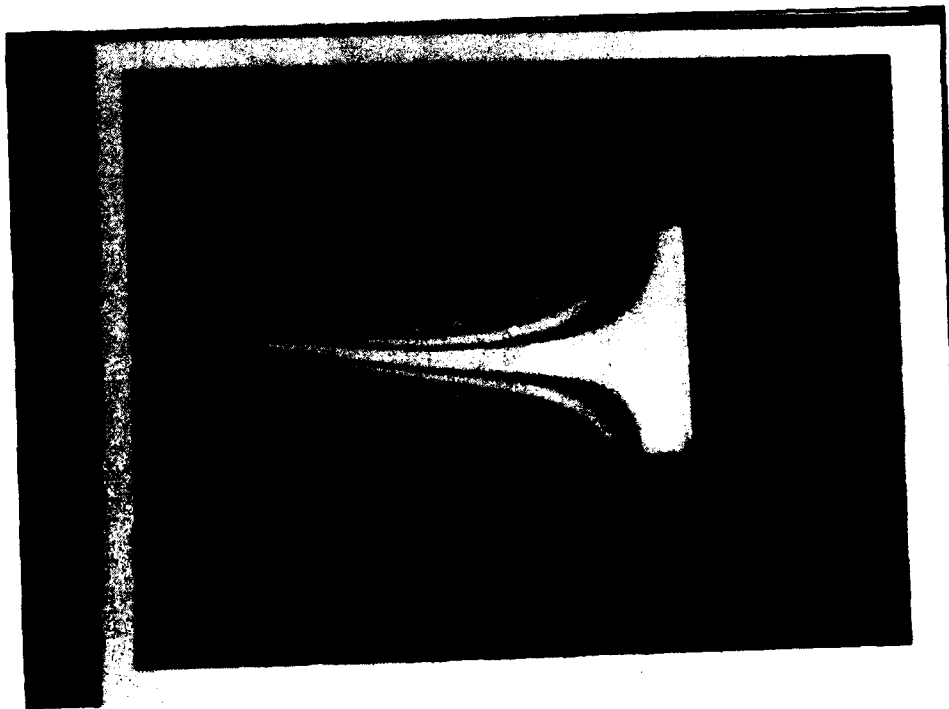


Figure 3.3.3.: Comparison of Test Holograms and Analytical Results for Mode 3

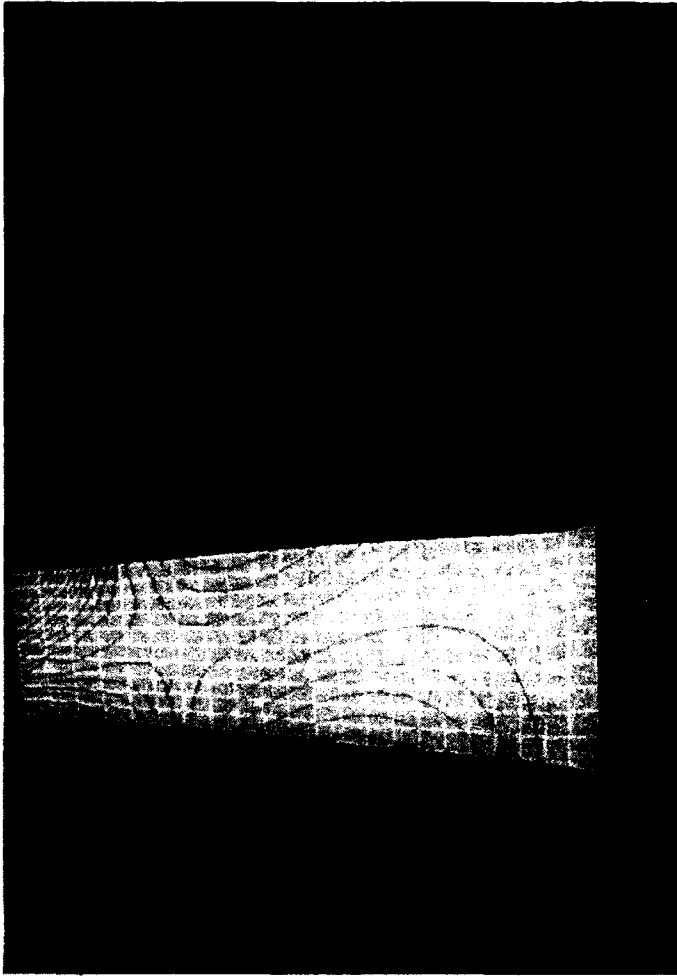
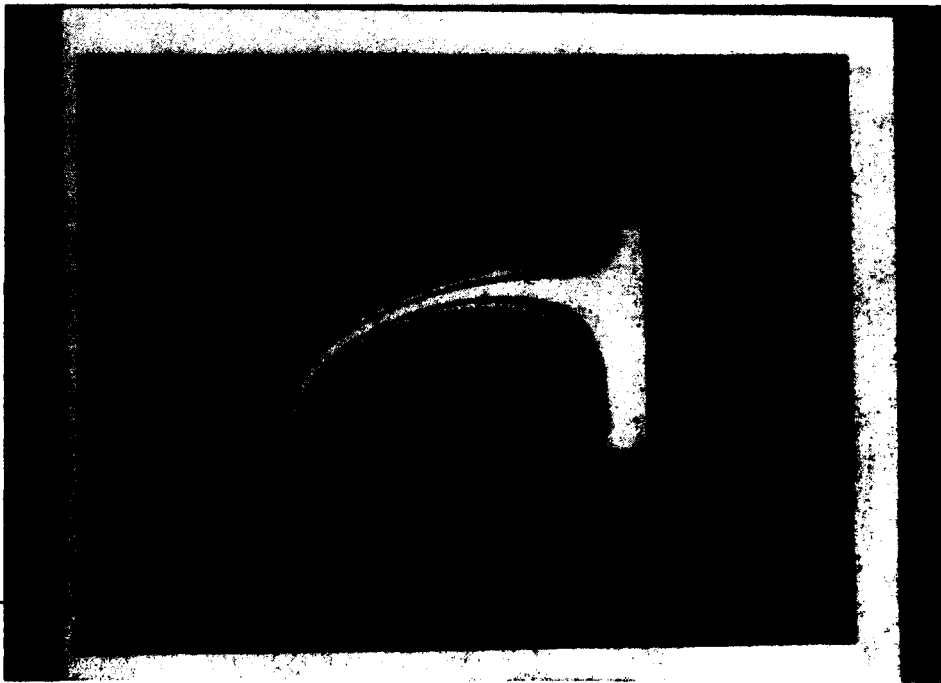


Figure 3.3.4: Comparison of Test Holograms and Analytical Results for Mode 5

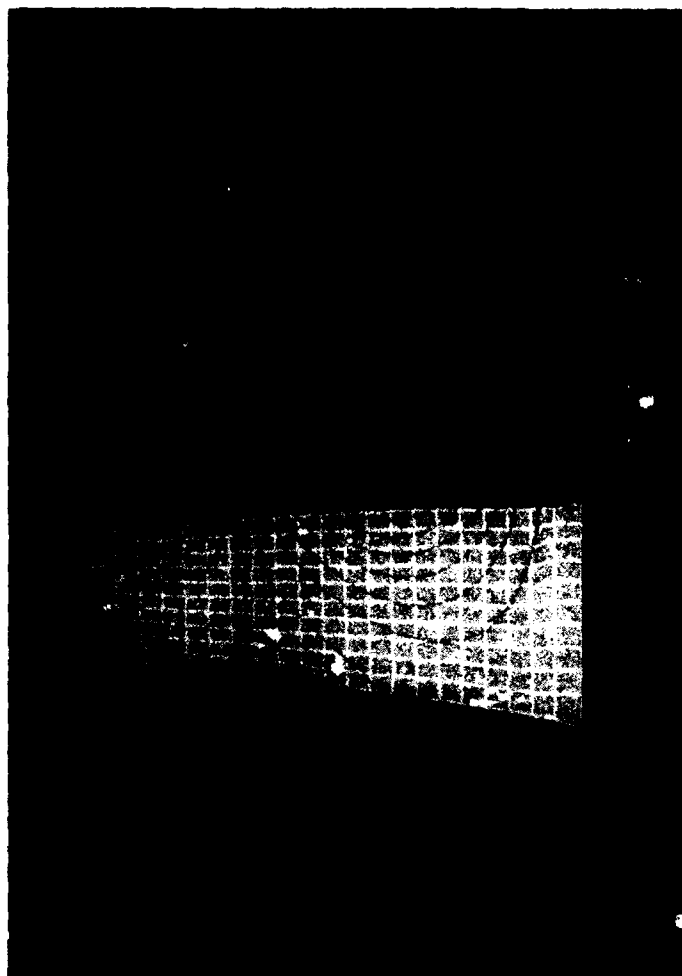
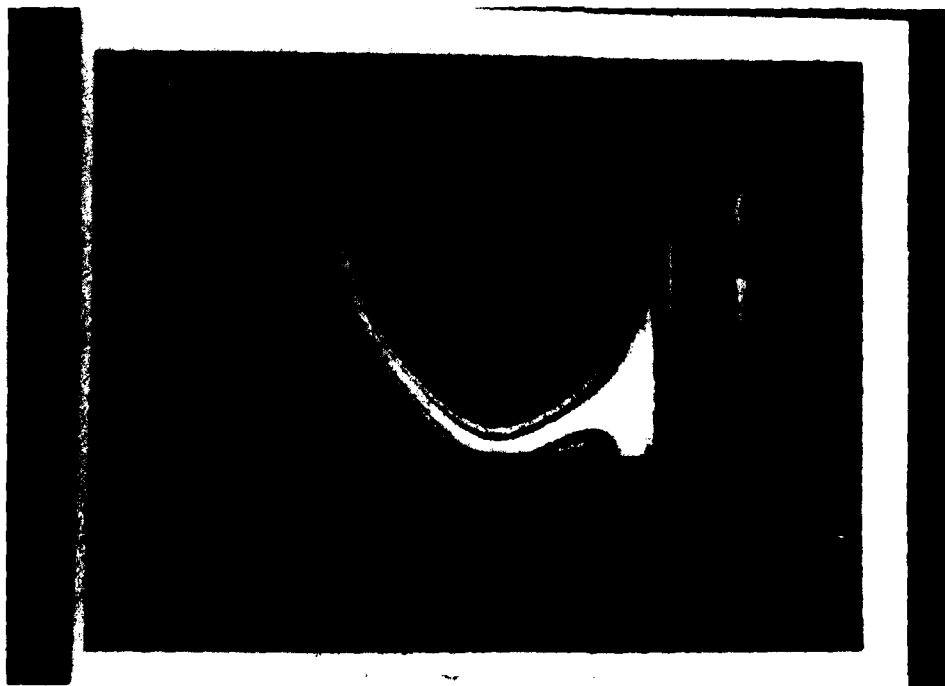


Figure 3.3.5: Comparison of Test Holograms and Analytical Results for Mode 6

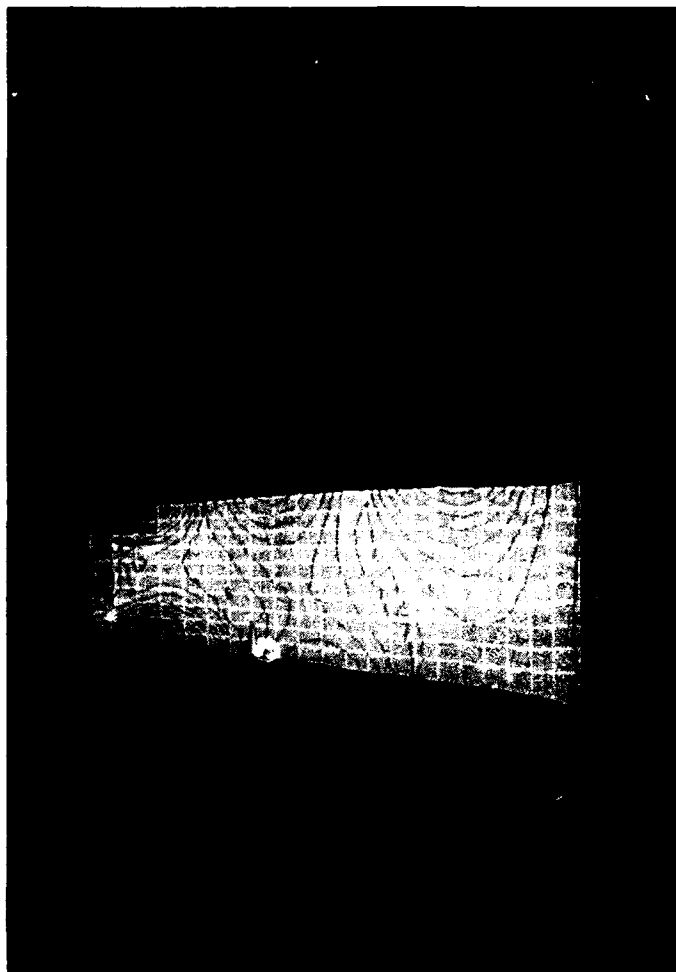


Figure 3.3.6: Comparison of Test Holograms and Analytical Results for Mode 8

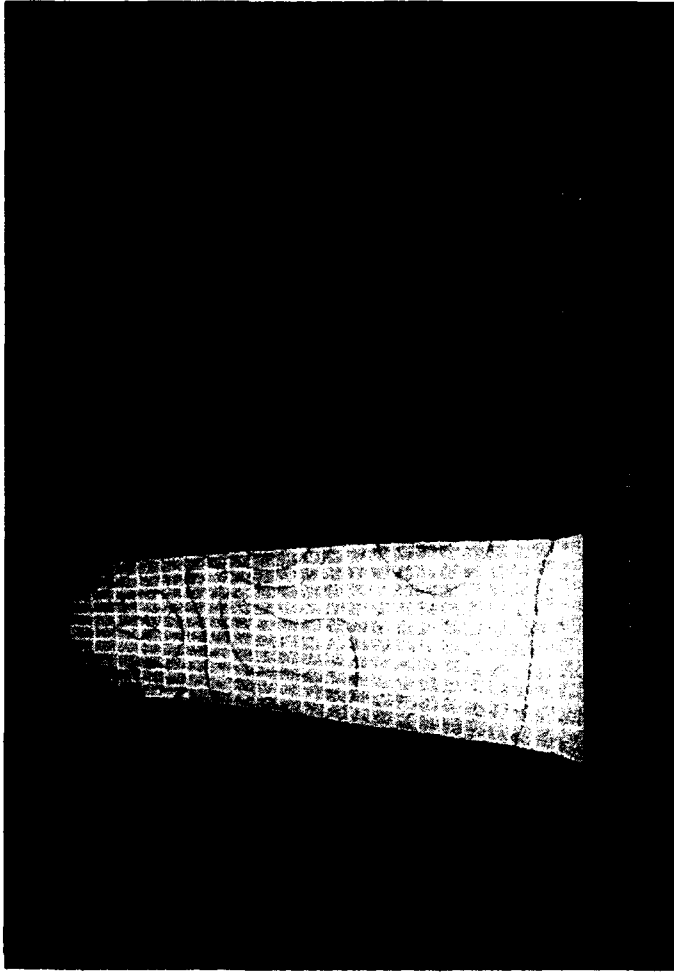
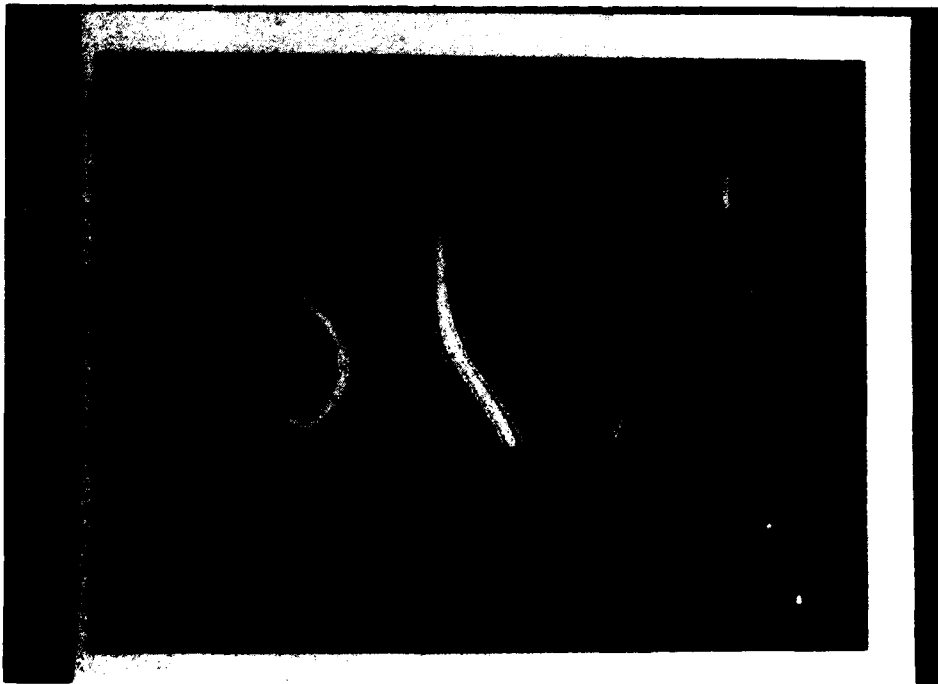


Figure 2.2.7: Comparison of Test Holograms and Analytical Results for Mode 10